

Programming Languages, Graphs, and more!

What was your favorite part about working on your
final project?

PollEv.com/cs106bpolls



What was your favorite part about working on your final project?



Roadmap

C++ basics

User/client

vectors + grids

stacks + queues

sets + maps

Core
Tools

testing

algorithmic
analysis

recursive
problem-solving

Object-Oriented
Programming

Implementation

arrays

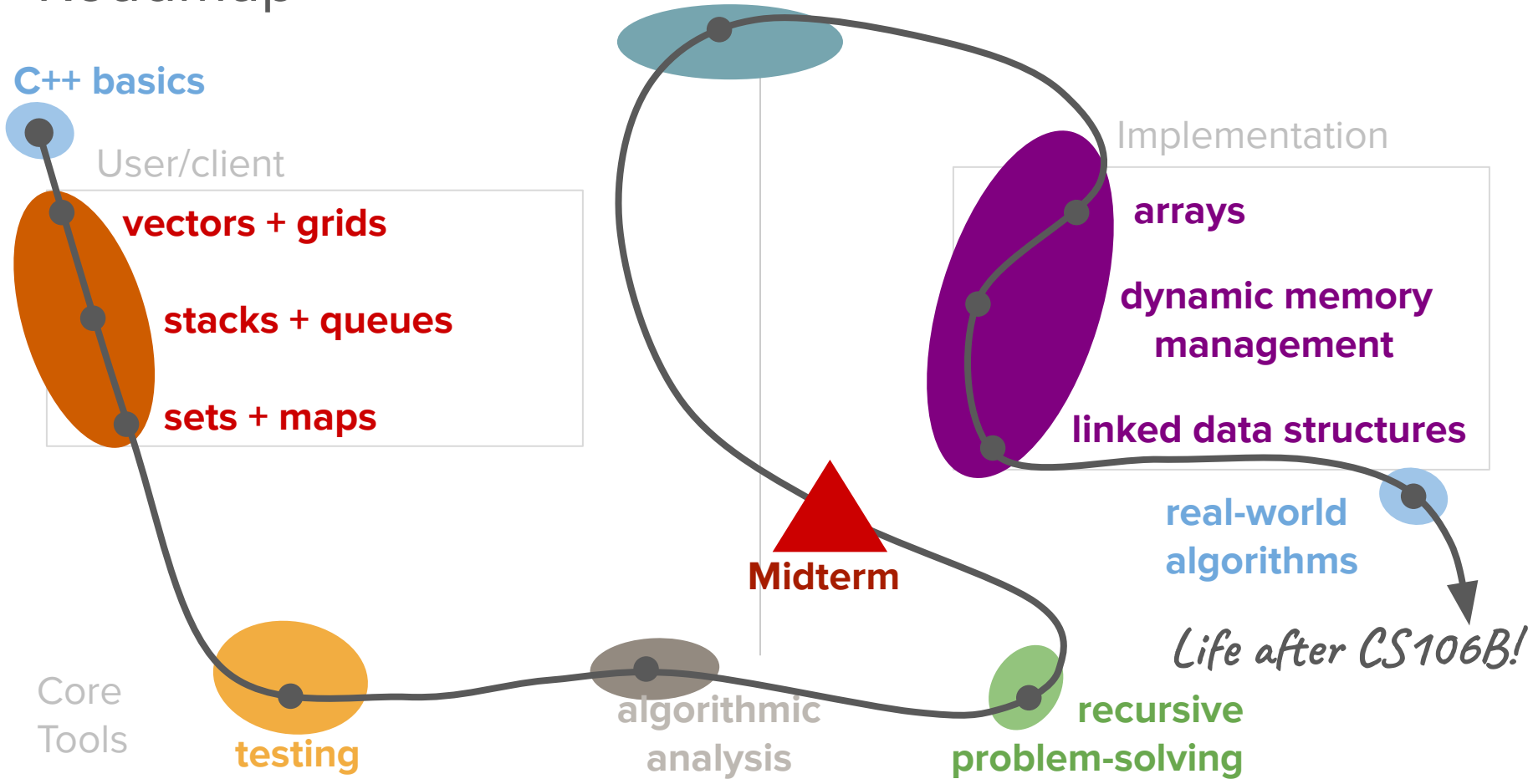
dynamic memory
management

linked data structures

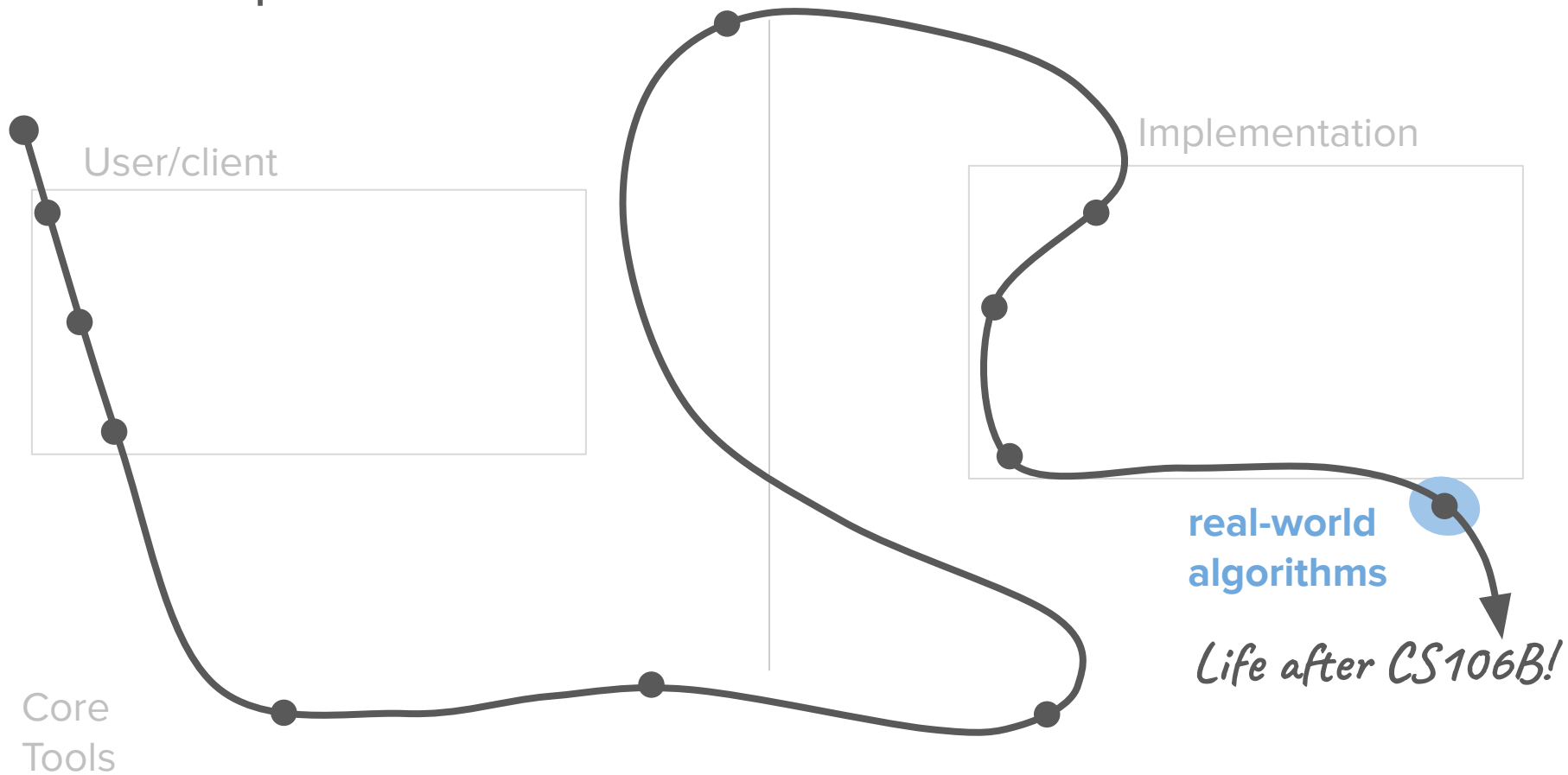
real-world
algorithms

Life after CS106B!

Midterm



Roadmap



Today's questions....by popular vote!

Why is programming language design like high fashion?

How can we represent real-world systems of connected components?

How do you start your own C++ projects?

Today's topics

1. Programming Languages
2. Graphs
3. Making your own C++ projects

Programming Language Design

C++ is a “a general-purpose programming language”
with “object-oriented, generic, and functional
features”

What does that mean?

Why is C++ this way?

What were the alternatives??

**YES THERE WERE
ALTERNATIVES**



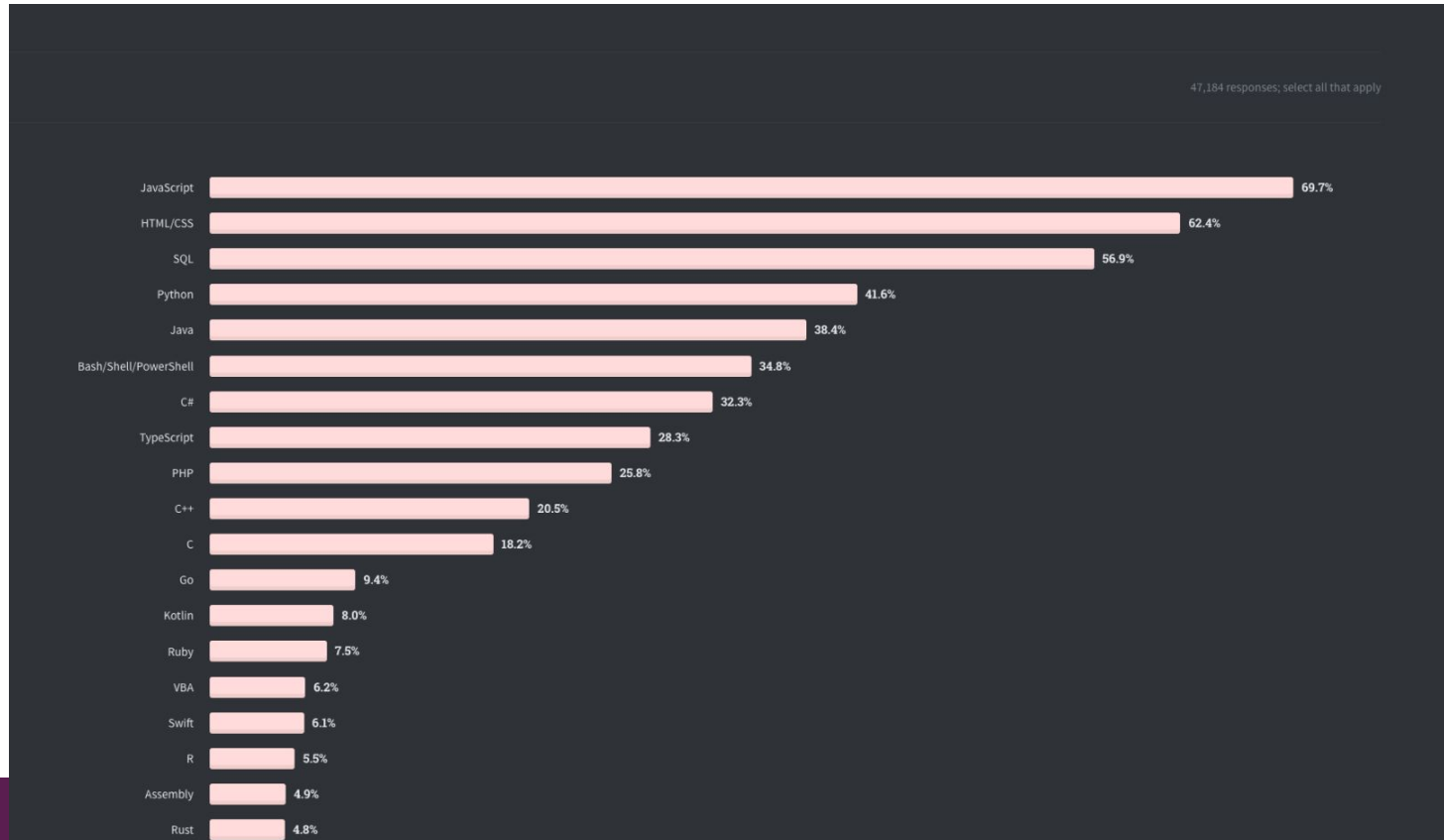
Shout out to Will Crichton who let us adapt
the following slides from CS242!

Guess the most popular programming language
(for professional developers) in 2020

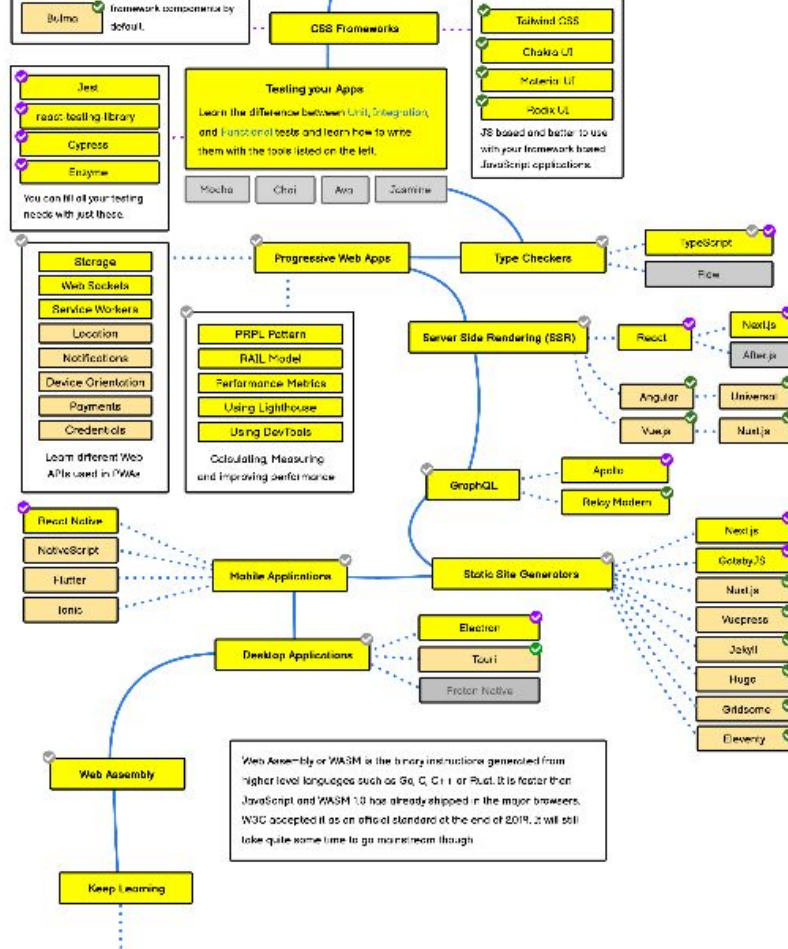
Guess the most popular programming language!



It's Javascript! (Stack Overflow, 2020)



Software



std::move_if_noexcept

Defined in header `<utility>`

```
template< class T >
typename std::conditional<
    !std::is_nothrow_move_constructible<T>::value && std::is_copy_constructible<T>::value,
    const T&,
    T&&
>::type move_if_noexcept(T& x) noexcept;
(since C++11)
(until C++14)

template< class T >
constexpr typename std::conditional<
    !std::is_nothrow_move_constructible<T>::value && std::is_copy_constructible<T>::value,
    const T&,
    T&&
>::type move_if_noexcept(T& x) noexcept;
(since C++14)
```

`move_if_noexcept` obtains an rvalue reference to its argument if its move constructor does not throw exceptions or if there is no copy constructor (move-only type), otherwise obtains an lvalue reference to its argument. It is typically used to combine move semantics with strong exception guarantee.

Parameters

x - the object to be moved or copied

Return value

`std::move(x)` or `x`, depending on exception guarantees.

Notes

This is used, for example, by `std::vector::resize`, which may have to allocate new storage and then move or copy elements from old storage to new storage. If an exception occurs during this operation, `std::vector::resize` undoes everything it did to this point, which is only possible if `std::move_if_noexcept` was used to decide whether to use move construction or copy construction. (unless copy constructor is not available, in which case move constructor is used either way and the strong exception guarantee may be waived)

Example

Run this code

```
#include <iostream>
#include <utility>

struct Bad
{
    Bad() {}
    Bad(Bad&&) // may throw
    {
        std::cout << "Throwing move constructor called\n";
    }
}
```


Guess the most popular programming
language in 1952

Guess again!

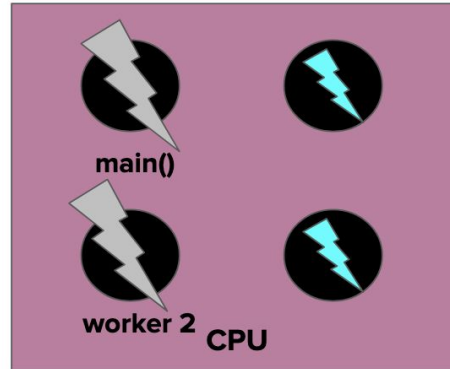


None! Only assembly languages

```
MOV AL, 1h      ; Load AL with immediate value 1
MOV CL, 2h      ; Load CL with immediate value 2
MOV DL, 3h      ; Load DL with immediate value 3
```

The syntax of MOV can also be more complex as the following examples show.^[24]

```
MOV EAX, [EBX]  ; Move the 4 bytes in memory at the address contained in EBX into EAX
MOV [ESI+EAX], CL ; Move the contents of CL into the byte at address ESI+EAX
MOV DS, DX      ; Move the contents of DX into segment register DS
```



And before that... raw numeric machine codes!!!

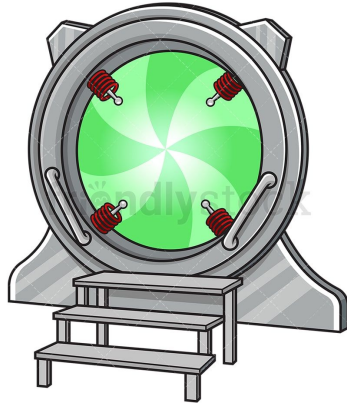


Grace Hopper
HOPL Keynote, 1978

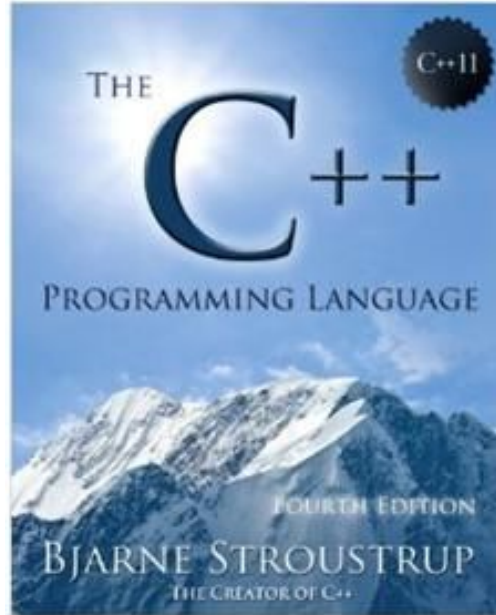
On assembly:

I think I spent 20 years fighting the "Establishment." In the early years of programming languages, the most frequent phrase we heard was that the only way to program a computer was in octal. Of course, a few years later a few people admitted that maybe you could use assembly language.

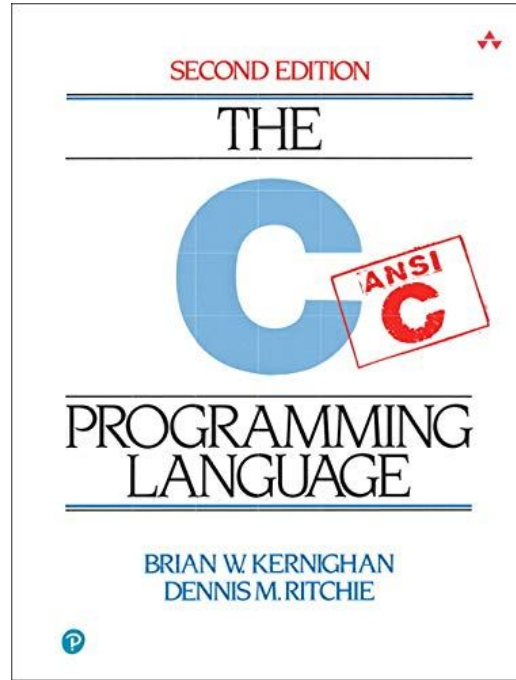
How did we get to 2022?



How did we get here? (C++, 1979)

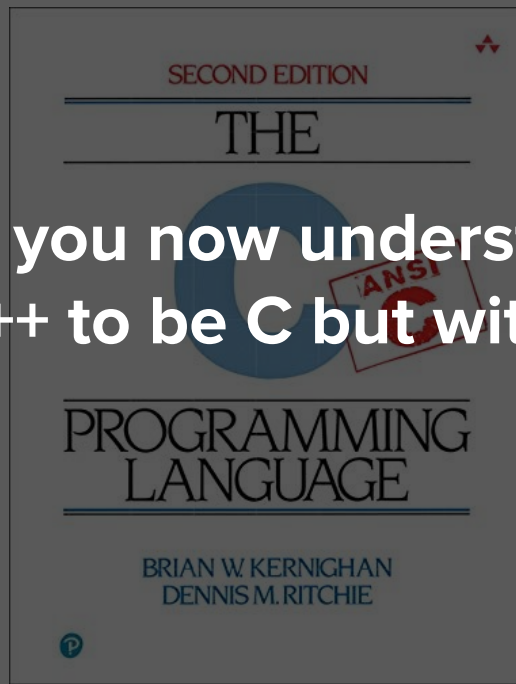


How did we get here? (C, 1972)

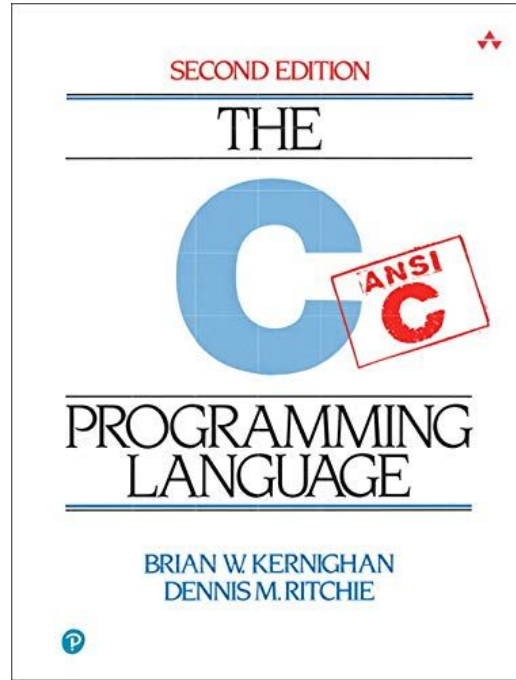


How did we get here? (1972)

Hey! Week 8 you now understands what it means for C++ to be C but with classes!



How did we get here? (C, 1972)



How did we get here? (B, 1969)

Article

Talk

Read

Edit

View history

B (programming language)

From Wikipedia, the free encyclopedia

This article is about a language.

B is a [programming language](#) developed by Ken Thompson.

B was derived from [BCPL](#), and its name might be based on Bon, an earlier programming language.

B was designed for recursive, non-lexical scoping, with the only data type being an integer.

In the context of the language, the word was treated either as an [integer](#) or a [memory address](#).

As machines with [ASCII](#) processing became common, notably the [DEC PDP-11](#) that arrived at Bell, support for character data stuffed in memory words became important. The typeless nature of the language was seen as a disadvantage, which led Thompson and Ritchie to develop an expanded version of the language supporting new internal and user-defined types, which became the [C programming language](#).

Contents [\[hide\]](#)

- [History](#)
- [Examples](#)
- [See also](#)



For more information, see [ABC \(programming language\)](#). For a list of other languages, see [List of programming languages](#).

Ken Thompson speculated that the name B was chosen for use on [Multics](#).^[note 1]

B was used to develop language software.^[3] It was a typeless language, with the word being treated either that might be. Depending on the

How did we get here? (Algol, 1959)



Alan Perlis,
"The American Side of the
Development of Algol" 1978

Algol introduced into programming languages such terms as type, declaration, identifier, for statement, while, if then else, switch, the begin end delimiters, block, call by value and call by name, typed procedures, declaration scope, dynamic arrays, side effects, global and local variables.

Algol was strongly derived from FORTRAN and its contemporaries. The logic, arithmetic and data organizations were close to those then being designed into real computers. Certain simple generalizations of computer instructions such as switch, for statement, and if statements were included because their semantics and computer processing were straight-forward consequences of single statement processing.

How did we get here? (Algol, 1959)



Alan Perlis,
"The American Side of the
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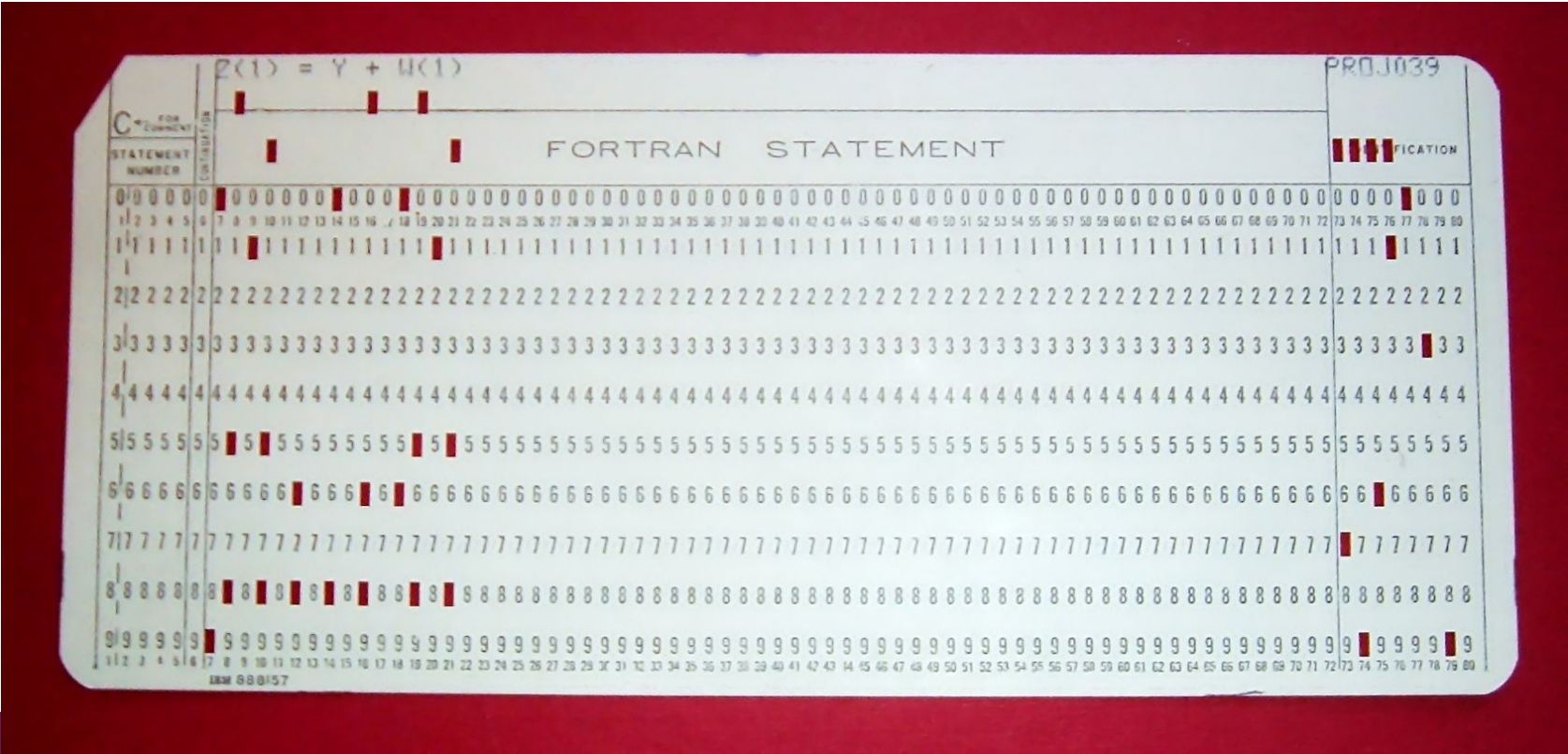
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*Type, variables,
for-loops, dynamic
arrays,
while-loops,
if-then-else, call
by ref vs value...*

*All things we still
use!*

How did we get here? (Fortran, 1957)



The starter code:

IBM **FORTRAN Coding Form** IBM 709-1
Printed in U.S.A.

PROGRAM		PUNCHING INSTRUCTIONS		GRAPHIC PUNCH		PAGE OF																																																																										
PROGRAMMER	DATE					CARD SEQUENCE NUMBER*																																																																										
STATEMENT NUMBER	LINE	FORTRAN STATEMENT																		IDENTIFICATION																																																												
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	

* A punched card form, IBM Form 4881-1, is available for punching statements from this form.

Fortran... kind of looks familiar!

```
1 PROGRAM main
2
3     IMPLICIT NONE
4
5     character(len = 15) :: hello = "Hello, World!"
6     print *, hello
7
8 END PROGRAM main
```

The big ideas in our programming languages haven't really changed since 1958.

statements, variable assignment, for loops, classes, and so on

Turing languages

1957 – FORTRAN

1959 – ALGOL

1962 – SIMULA

1972 – C

1979 – C++

1991 – Python

1995 – Java



It didn't need to be this way!



And in fact, it hasn't!



Turing languages

1957 – FORTRAN

1959 – COBOL, ALGOL

1962 – SIMULA

1972 – C, Smalltalk

1979 – C++

1991 – Python

1995 – Java

1959 – LISP

1966 – ISWIM

1972 – Prolog

1978 – ML

1990 – Haskell

Alan Turing



"On Computable Numbers" 1937

Alonzo Church



"A set of postulates for the foundation of logic", 1932

What do you think this does? What do you observe?

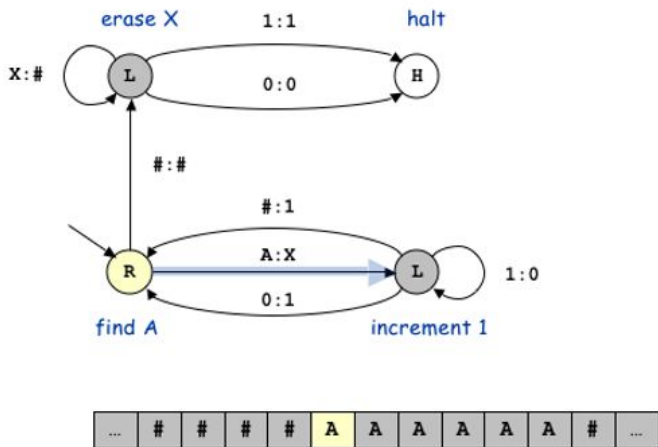
```
1  #lang racket
2
3  (define (extract str)
4    (substring str 4 7))
5
6  (extract "the cat out of the bag")
```

```
4 ;; Push elem onto stack (default value null).
5 (define (push elem [stack null])
6   (cons elem stack))
7
8 ;; Pop item off stack, returning the stack after pop.
9 (define (pop stack)
10  (unless (empty? stack)
11    (rest stack)))
12
13 ;; Peek at top element of stack, returning it.
14 (define (peek stack)
15  (unless (null? stack)
16    (first stack)))
17
18 ;; Run a program defined as a stack.
19 (define (run prog)
20  ;; Internal stack.
21  (define stack null)
22  ;; for each element in program..
23  (for ([elem prog])
24    ;; if current element is a procedure..
25    (if (procedure? elem)
26        ;; local bindings for the top two elements..
27        (let ([num1 (peek stack)]
28              [num2 (peek (pop stack))])
29            ;; set! the internal stack to be the current stack with top two
30            ;; elements popped off and the result of applying current elem to them
31            ;; pushed to stack.
32            (set! stack (push (elem num1 num2) (pop (pop stack)))))
33        ;; Otherwise, set! the internal stack to the result of pushing the
34        ;; current element to the stack.
35        (set! stack (push elem stack))))
36  stack)
37
```


Turing languages

Inspired by computers
Computation as operations on a machine

Turing machines



Church languages

Inspired by math!
Computation as mathematical functions

Lambda calculus

$$\begin{aligned} [x \rightarrow y] x &= y \\ [x \rightarrow y] z &= z \\ [x \rightarrow y] \lambda z . x &= \lambda z . y \\ [x \rightarrow y] \lambda y . x y &= \lambda y' . y y' \\ [x \rightarrow y] x (\lambda x . x) &= y (\lambda x . x) \end{aligned}$$

Turing languages

- **Focus on practical connection to computers**
 - Make hardware first, then design software abstractions around that
 - How does data get stored?
 - What is the order of execution (control of flow)?

Church languages

- **Focus on mathematics**
 - Think through abstractions first. What is the “mathematical essence of a function” first?
 - What is a function?
 - How can we formally define functions?
 - How can we formally define variables?

Key idea

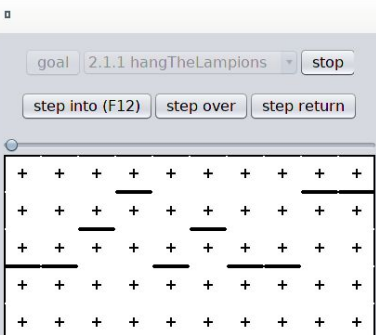
Programming paradigm: a way we cluster languages by a combination of programming style and language behavior

Imperative paradigm

```

/home/fred/karel/!karel.txt
1 void hangTheLampions()
2 {
3     repeat (9)
4     {
5         hangOneLampion();
6         moveForward();
7     }
8     hangOneLampion();
9 }
10
11 void hangOneLampion()
12 {
13     turnLeft();
14     pickBeeper();

```



Functional paradigm

F	G	H	I	J	K
-'14					
1st Quarter	Average	Number Grade			95.5
96	92.5	=IF(G3>89,"A",IF(G3>79,"B",IF(G3>69,"C",IF(G3>59,"D",IF(G3<60,"F"))))			
85	78	C[logical_test, value_if_true, value_if_false]			85.15625
90	81	B			84
90	87.25	B			79.75
91	79.75	B			83.25
99	95.5	A			79.75
89	84	B			79.75
95	83.25	B			
					#NUM!
Class Average	85.15625	B			

Object-oriented paradigm

```

#pragma once
#include "vector.h"
class RandomBag {
public:
    void add(int value);
    int removeRandom();

private:
    Vector<int> elems;
};

```

How do we compare across
languages?

What should we compare across languages?

Are these two types of languages
equally powerful?

Key idea

Church Turing Thesis: Anything that you could compute with a Turing Machine you could compute with lambda calculus.

Key idea

Turing complete: equivalent computational power to a Turing machine...aka any algorithm could be implemented

Used as a benchmark for what kind of stuff you can do with a programming language

Key idea

Turing complete: equivalent computational power to a Turing machine...aka any algorithm could be implemented

Used as a benchmark for what kind of stuff you can do with a programming language

Java

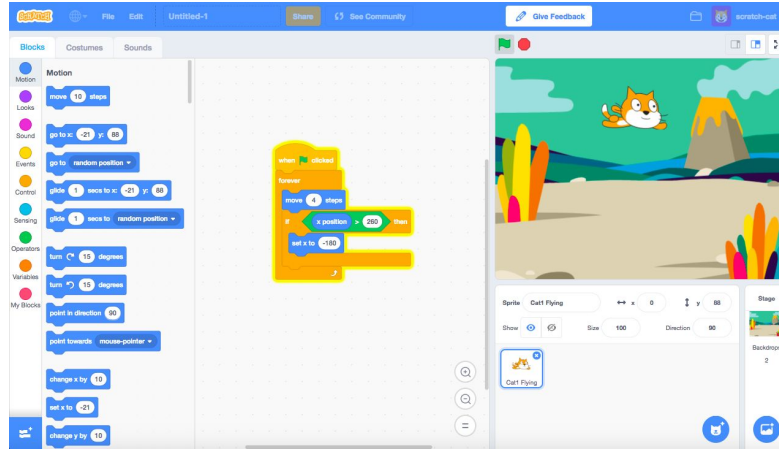
C++

Python

C

Which of these are NOT Turing complete?

Minecraft

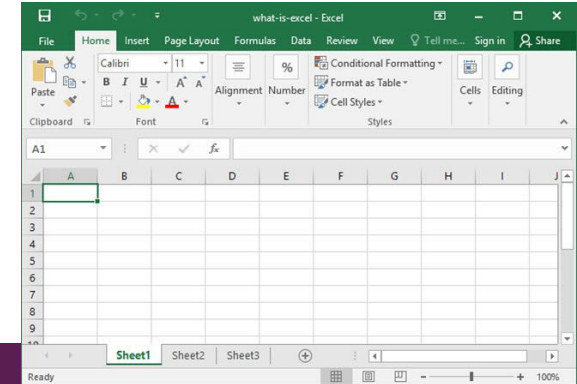


Scratch

HTML

```
1 <!DOCTYPE html>
2 <html>
3   <head>
4     <meta charset="UTF-8">
5     <title>Title goes here</title>
6   </head>
7   <body>
8
9   </body>
10 </html>
```

Excel



Which of these are NOT Turing complete?

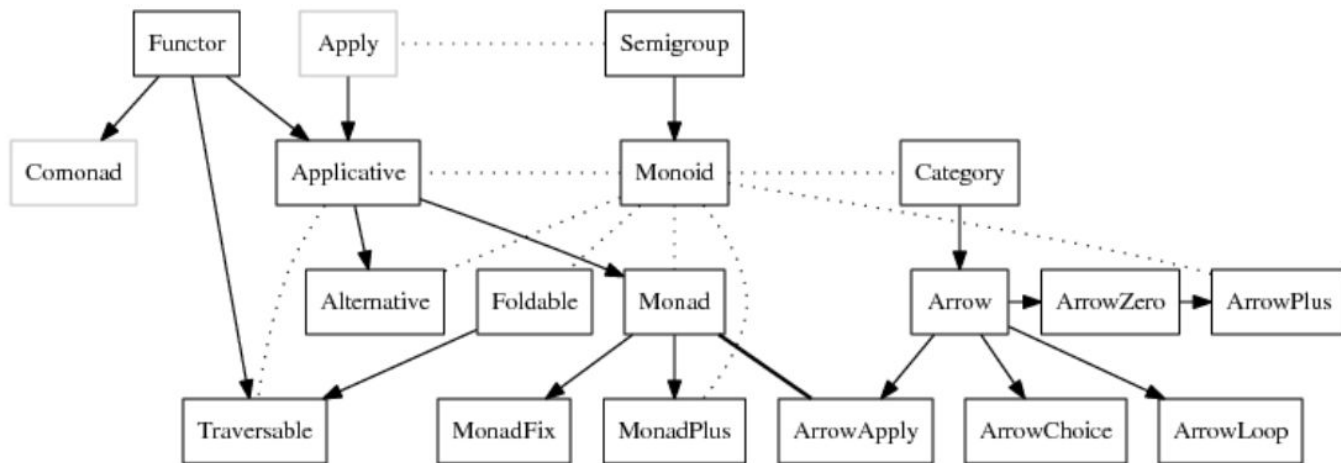
HTML

```
1  <!DOCTYPE html>
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6    </head>
7    <body>
8
9    </body>
10 </html>
```

- Describes data, not computation
- Doesn't allow you to execute for-loops, etc.
 - Not every algorithm can be implemented using HTML

Are these two types of languages
equally easy to use?

Church languages are intimidating



Couldn't match type `k0' with `b'

because type variable `b' would escape its scope

This (rigid, skolem) type variable is bound by

the type signature for

```
groupBy :: Ord b => (a -> b) -> Set a -> Set (b, [a])
```

The following variables have types that mention k0

```

public class Person {
    private final String firstName;
    private final String lastName;
    private final Integer age;
    public Person(String firstName,
                  String lastName,
                  Integer age) {
        this.firstName = firstName;
        this.lastName = lastName;
        this.age = age;
    }
    public String getFirst() {
        return firstName;
    }
    public String getLast() {
        return lastName;
    }
    public Integer getAge() {
        return age;
    }
    public Boolean valid() {
        return age > 18;
    }
}

public static List<String> validByAge(List<Person> in) {
    List<Person> people = new ArrayList<Person>();
    for (Person p: in) {
        if (p.valid()) people.add(p);
    }

    Collections.sort(people, new Comparator<Person>() {
        public int compare(Person a, Person b) {
            return a.age() - b.age();
        }
    });

    List<String> ret = new ArrayList<String>();
    for (Person p: people) {
        ret.add(p.first);
    }
    return ret;
}

List<Person> input = new ArrayList<Person>();
input.add(new Person("John", "Valid", 32));
input.add(new Person("John", "Invalid", 17));
input.add(new Person("OtherJohn", "Valid", 19));

List<Person> output = validByAge(input)

```

```

case class Person(val first: String, val last: String, val age: Int) {
    def valid: Boolean = age > 18
}

```

```

def validByAge(in: List[Person]) =
    in.filter(_.valid).sortBy(_.age).map(_.first)

```

```

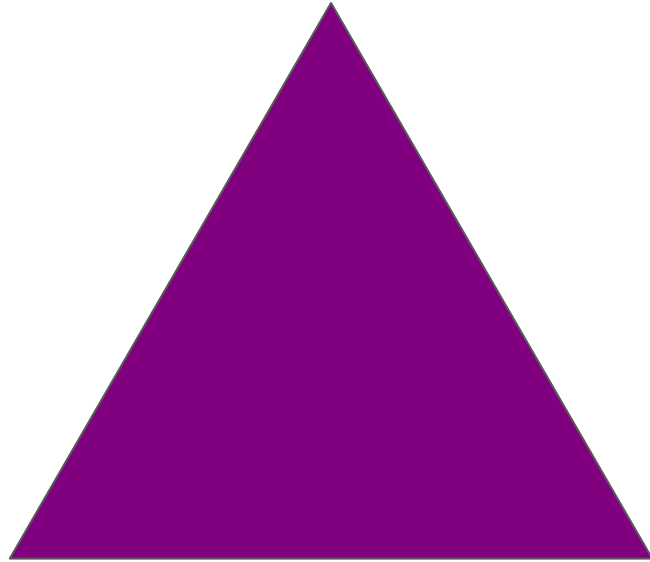
validByAge(List(
    Person("John", "Valid", 32),
    Person("John", "Invalid", 17),
    Person("OtherJohn", "Valid", 19)))

```

Other ways to compare
programming languages

Tradeoffs

Productivity

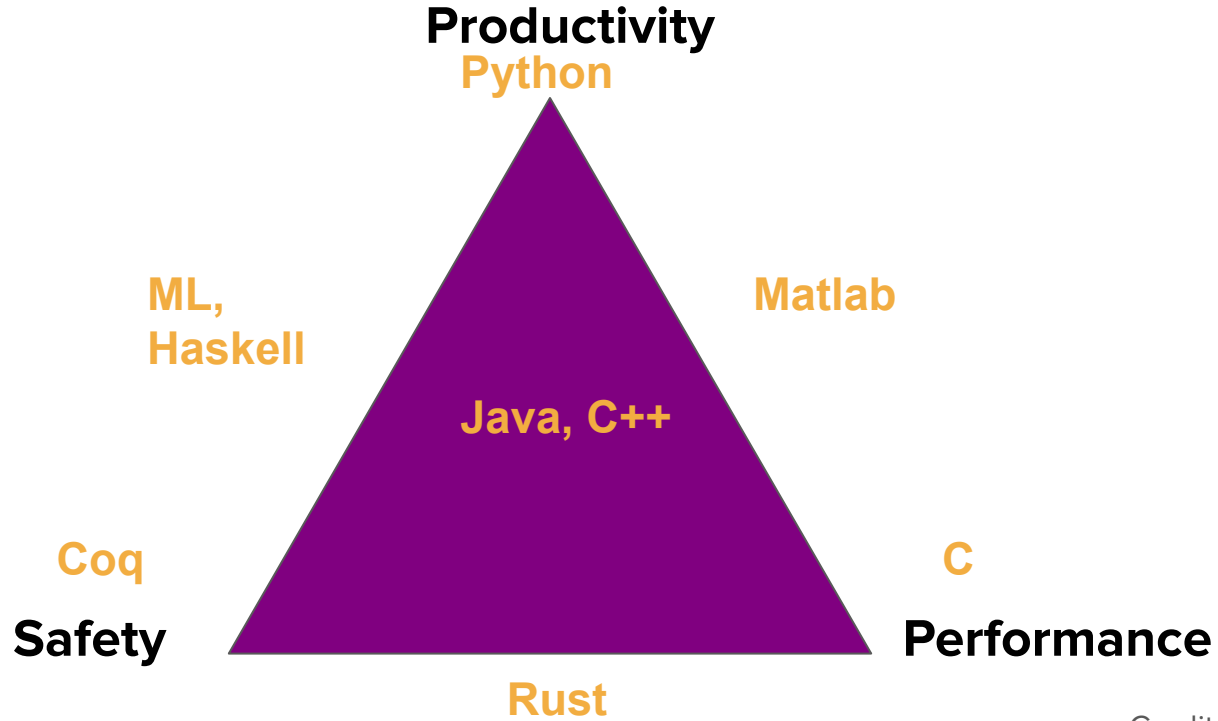


Safety

Performance

Credit: Alex Aiken

Tradeoffs



Credit: Alex Aiken

Design consideration: Productivity

Productivity:

- **Do we have big, easy-to-use building blocks (aka libraries) to get to powerful programs?**
- Is this programming language easy-to-use and read?

Productivity: libraries to build on top of?



python takes the cake!

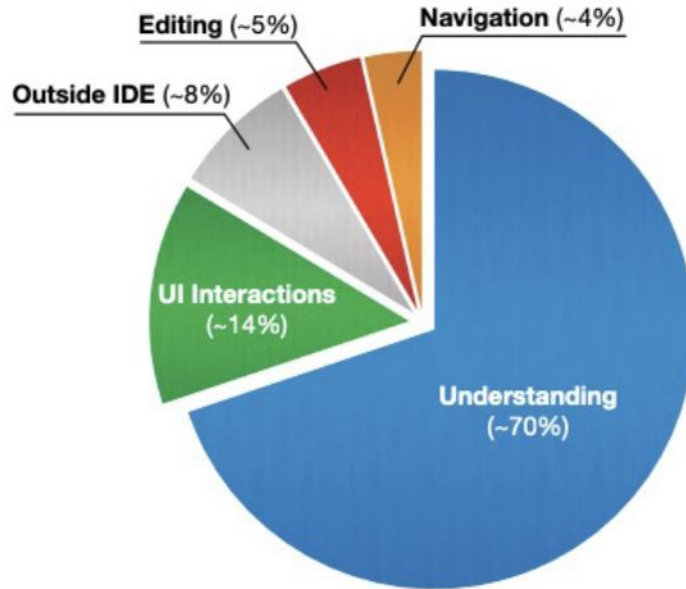
Productivity:

- Do we have big, easy-to-use building blocks (aka libraries) to get to powerful programs?
- **Is this programming language easy-to-use and read?**

What percentage of time do
programmers spend actually writing
code when they're programming?

ONLY 5%





Minelli et al. "I Know What You Did Last Summer: An Investigation of How Developers Spend Their Time" ICPC '15.

Project	Comprehension	Navigation	Editing	Others
Average	57.62%	23.96%	5.02%	13.40%

Xia et al. "Measuring Program Comprehension: A Large-Scale Field Study with Professionals." IEEE Trans. Softw. Eng, 2018.

Productivity:

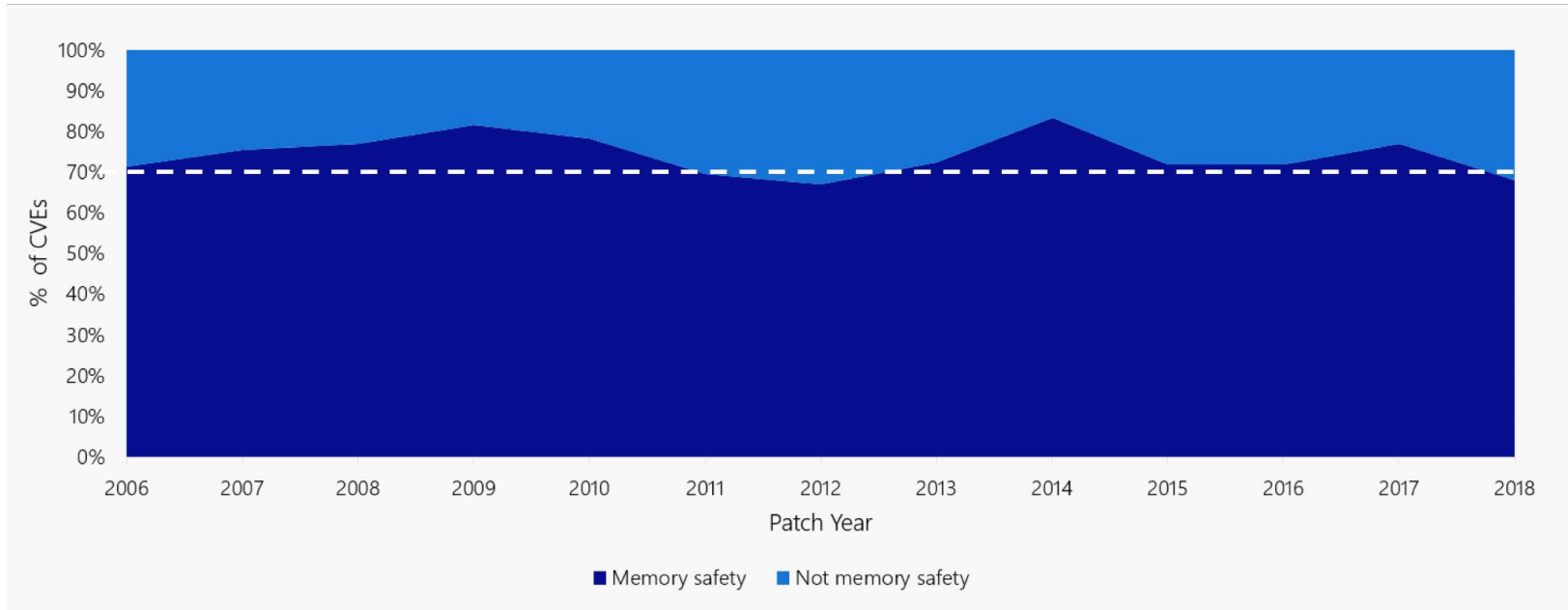
- Do we have big, easy-to-use building blocks (aka libraries) to get to powerful programs?
- Is this programming language easy-to-use and read?

Design consideration: Safety

Safety: reduce vulnerabilities,
exposures, errors

What percentage of Common Vulnerabilities and Exposures in C++ are caused by memory bugs?

"The majority of vulnerabilities fixed and with a CVE assigned are caused by developers inadvertently inserting memory corruption bugs into their C and C++ code."



Microsoft Security Response Center. "A proactive approach to more secure code." 2019

Womp womp

Buffer
(8 bytes)

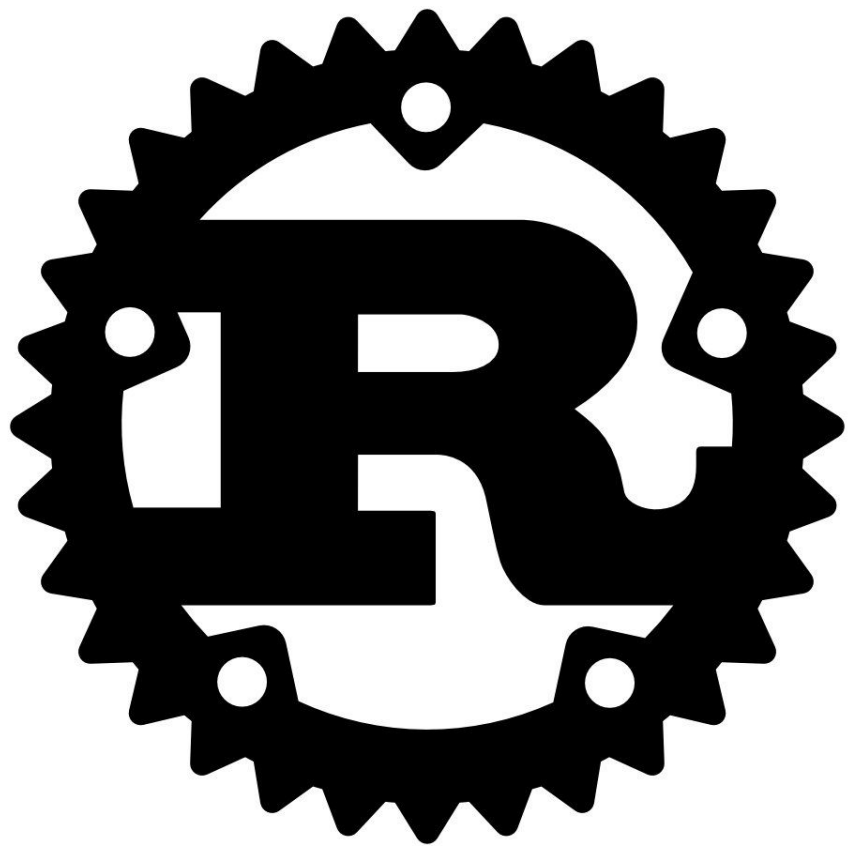
P	A	S	S	
0	1	2	3	

**EMMANUEL
DON'T
DO
IT**



reference a null pointer”

```
libraries: ■ FB■$■ET■  
n file or directory
```



The Rust Programming Language

Design consideration: Performance

How much faster is C compared to
Java?

	Immutable	Mutable	Double Only	No Objects	In C	Transposed	Tiled	Vectorized	BLAS MxM	BLAS Parallel
ms	17,094,152	77,826	32,800	15,306	7,530	2,275	1,388	511	196	58
	219.7x		2.2x		3.4x		2.8x		3.5x	
	2.4x		2.1x		1.7x		2.7x			
	219.7x									
	522x									
	1117x									
	2271x									
	7514x									
	12316x									
	33453x									
	87042x									
	296260x									
Cycles/OP	8,358	38	16	7	4	1	1/2	1/5	1/11	1/36

The Future of PLs

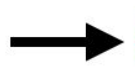


Designing cutting-edge programming languages is like designing high fashion

- Very few people will actually use the newest PLs out of PL research but the PL research is crucial to finding the boundaries / limits / new frontiers of programming as we know it
- There are trickle-down effects

Credit: Jean Yang

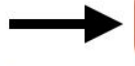
Church languages are coming!



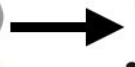
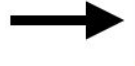
Scala +



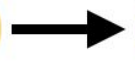
Objective-C



Swift



julia



(with types)

- Types!
- Memory safety!
- Better error handling!
- Better compilers!
- Better abstract patterns!
- Generic/modular programming!
- Concurrency / parallelization!

Church languages are coming!

Messenger.com Now 50% Converted to Reason

September 8, 2017

Boom!

- Messenger used to receive bugs reports on a daily basis; since the introduction of Reason, there have been a total of **10 bugs** (that's during the whole year, not per week)! *
- Most of the messenger core team's new features are now developed in Reason.
- Dozens of massive refactors while iterating on ReasonReact. Refactoring speed went from days to hours to dozens of minutes. I don't think we've caused more than a few bugs during the process (counted toward the total number of bugs).

Things we didn't cover in PL design

- Idea of programming paradigms
- Interpreted vs compiled language
- Static vs dynamic typing
- Usability / User Interactions
- Non-western traditions of computation

The future is out there!



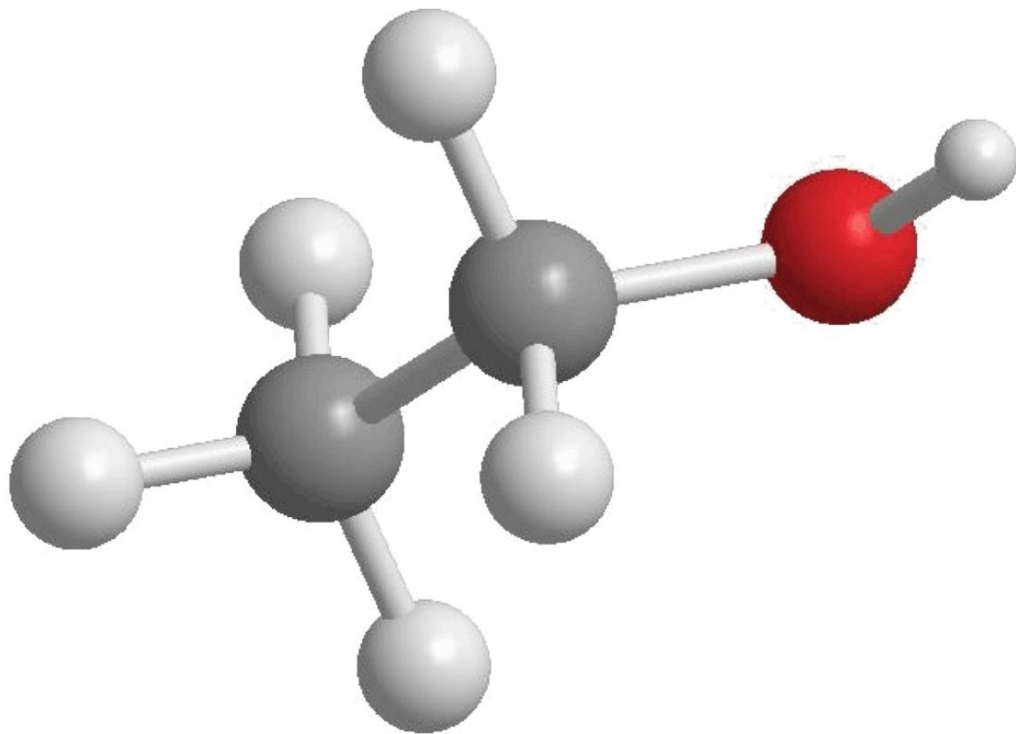
How can we represent
real-world systems of
connected components?

Graphs

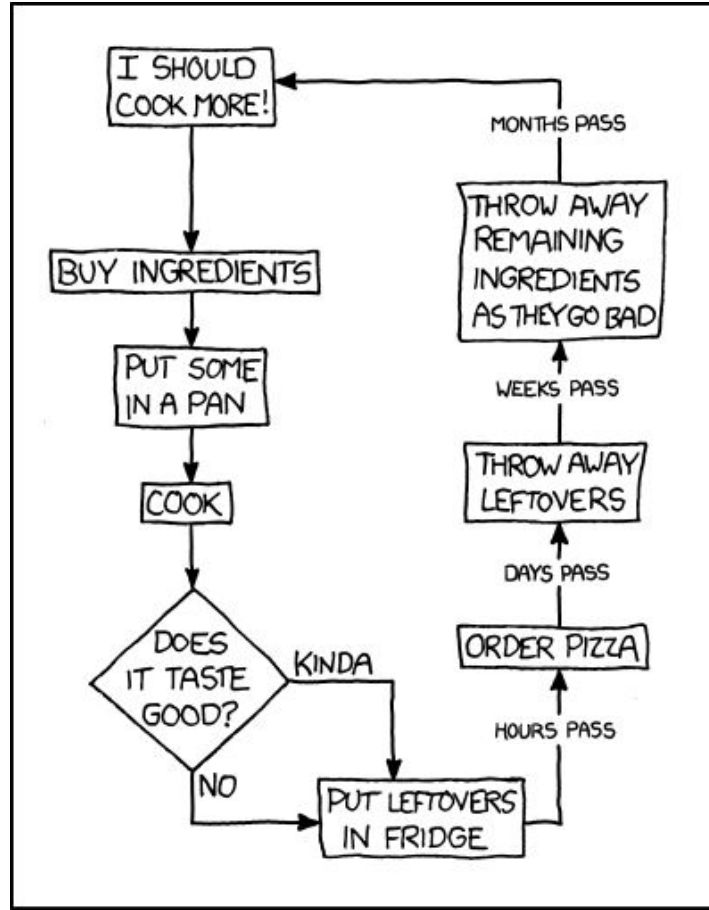
Social Networks



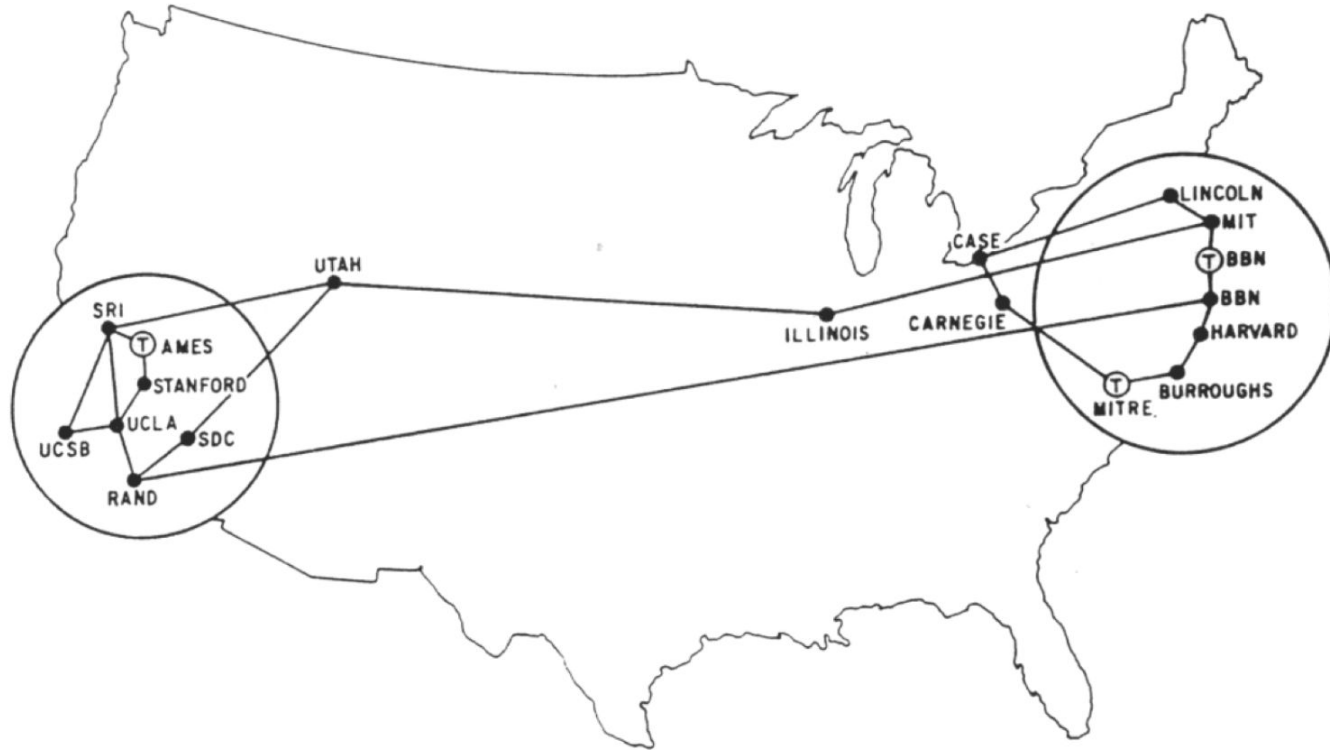
Chemical Bonds



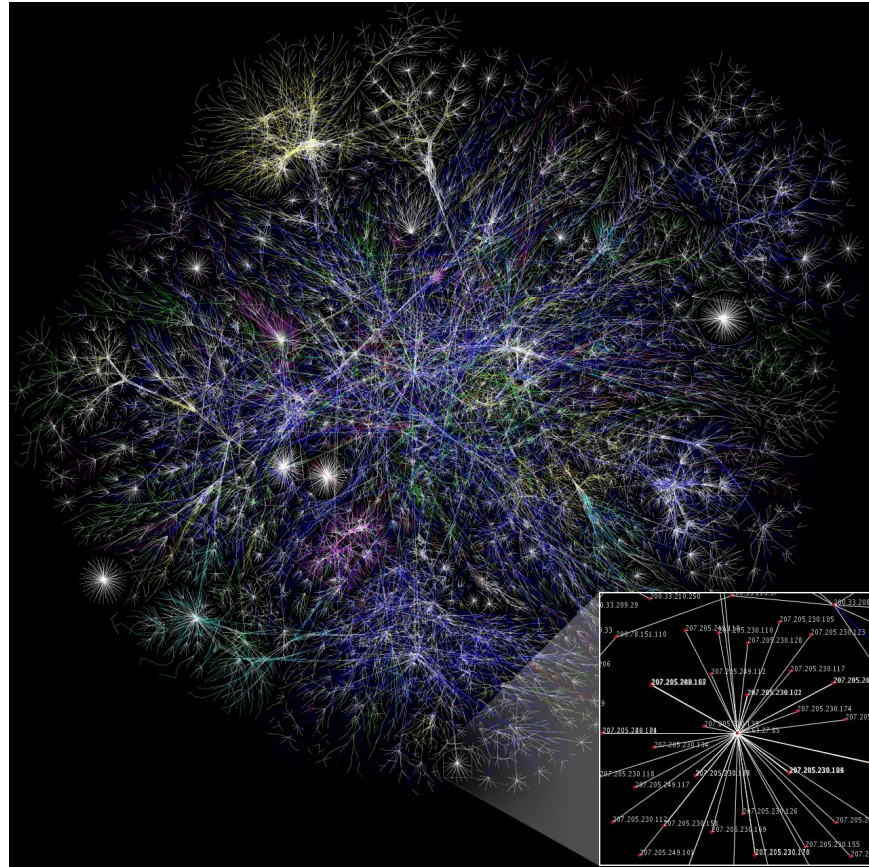
Flowcharts



The Internet!



The Internet!



What is a graph?

Definition

graph

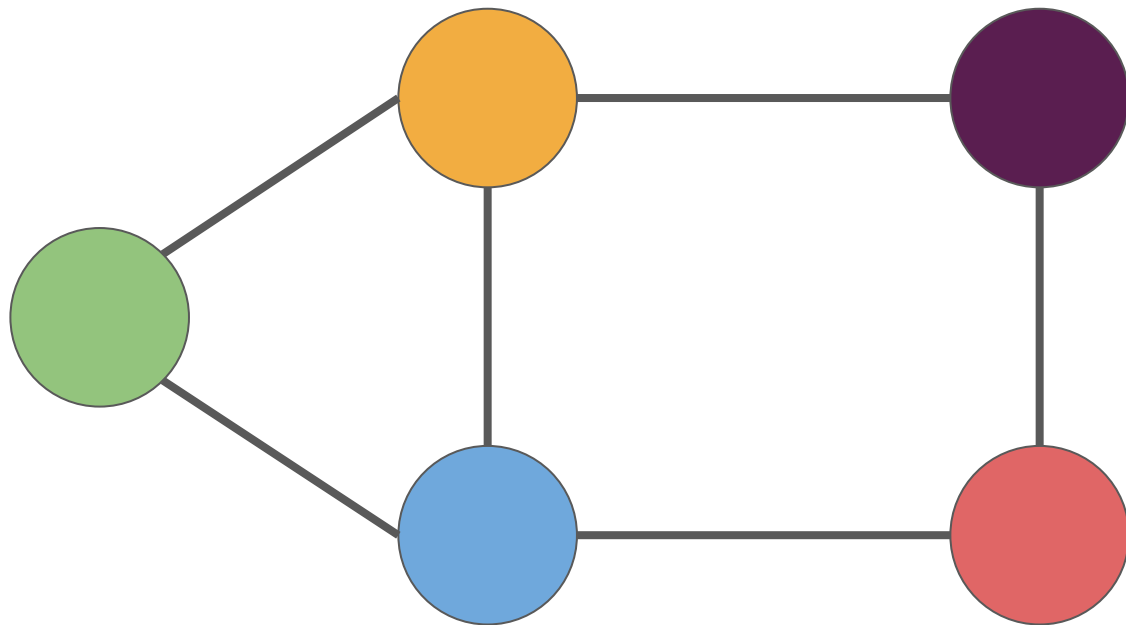
A structured way to represent relationships between different entities.

Our first graph!

- A structured way to represent relationships between different entities.

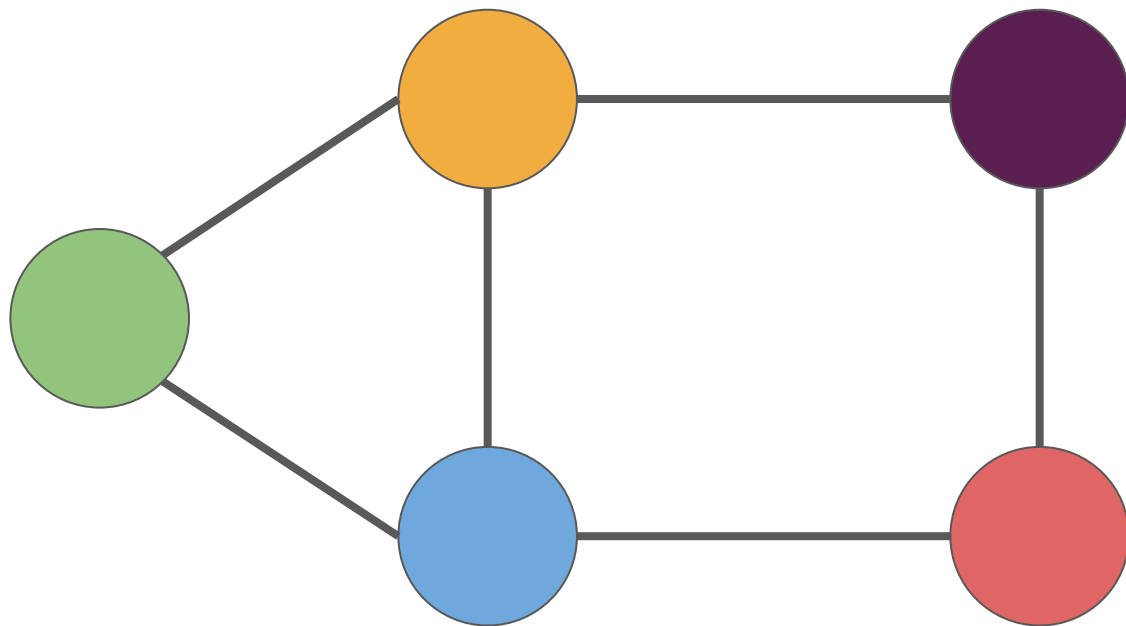
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Our first graph!

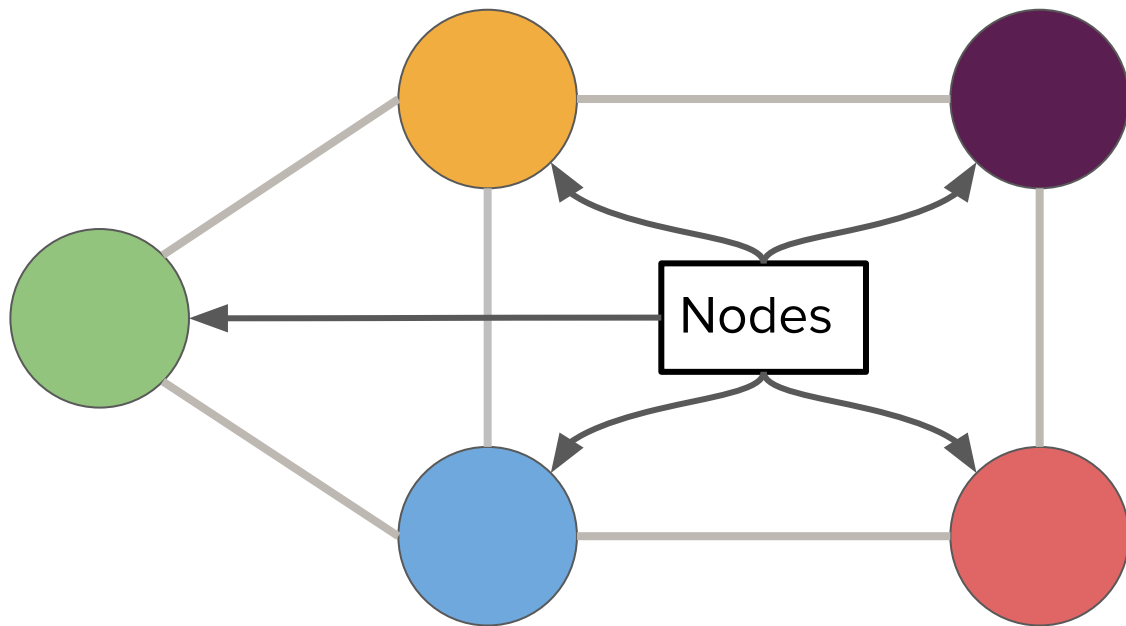
- A structured way to represent relationships between different entities.



A graph consists of a set of **nodes** connected by **edges**.

Our first graph!

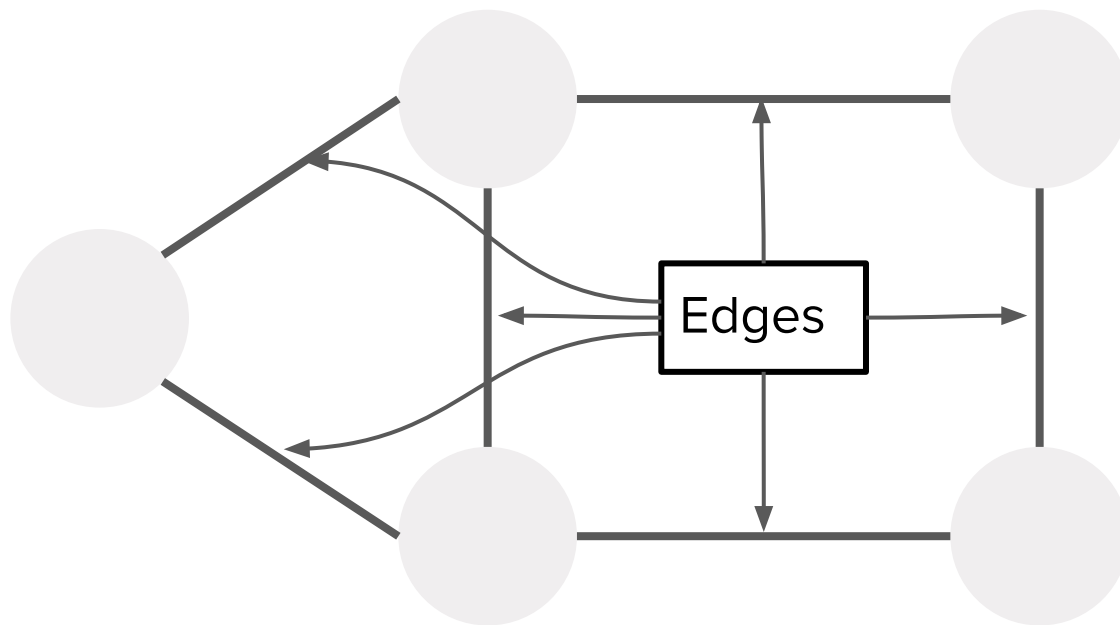
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Our first graph!

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Types of graphs

Different types of graphs

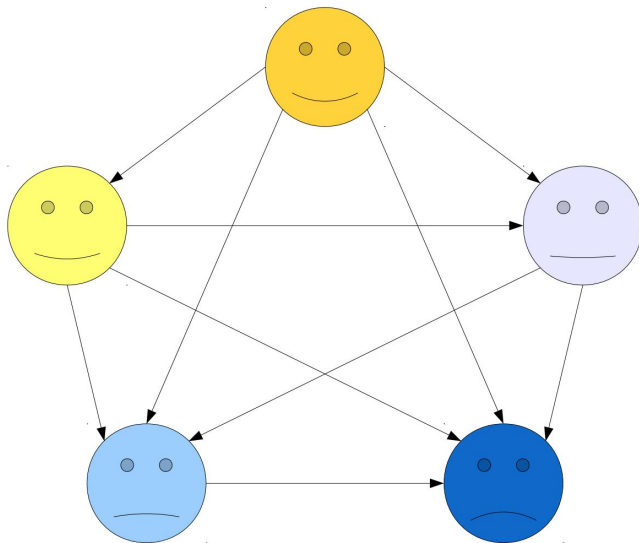
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 - Ex: I follow Dwayne "The Rock" Johnson on Instagram, but he doesn't follow me back.

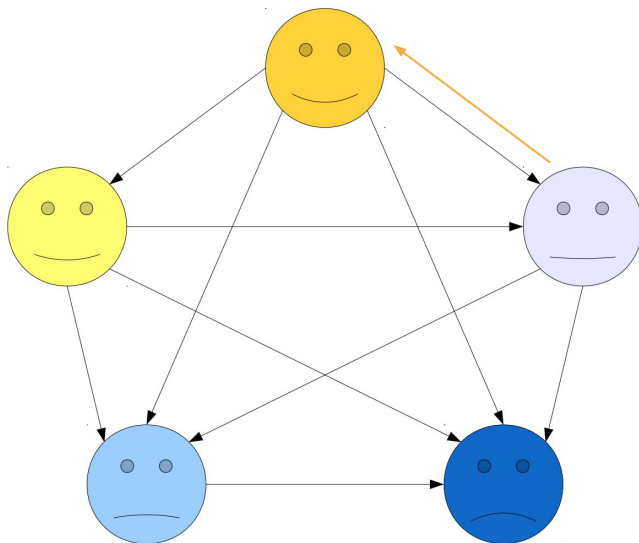
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Note: It is possible for a relationship in a directed graph to go both ways between two nodes, but it would need to be explicitly stated.

Different types of graphs

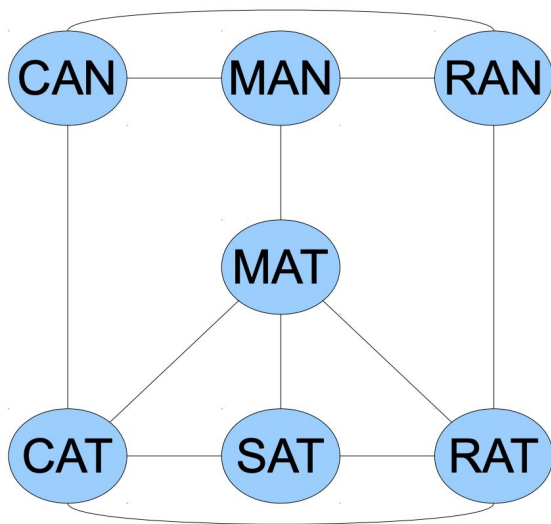
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Different types of graphs

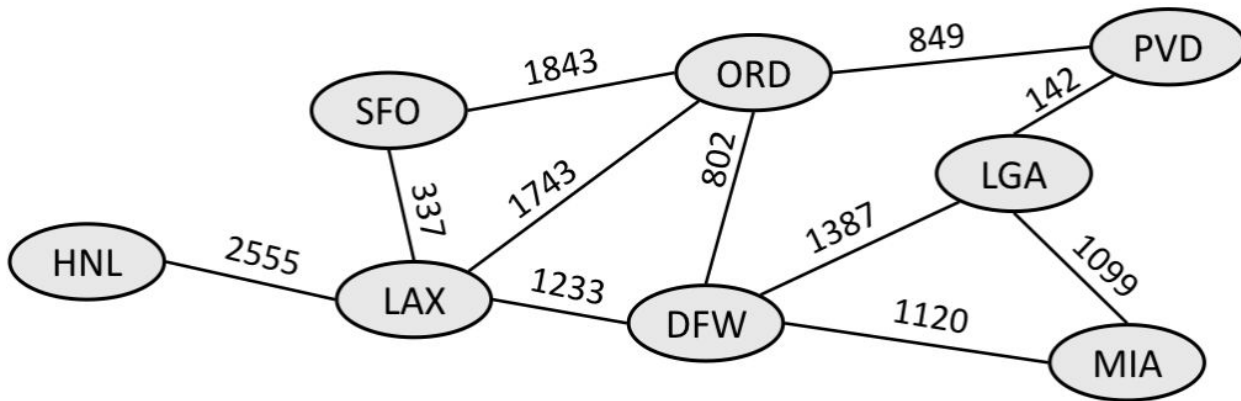
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 - Ex: The different bonds between atoms in a single molecule all have different bond energies and strengths.

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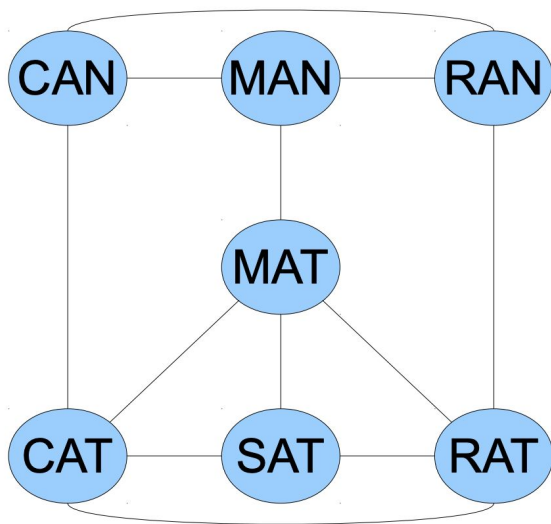


Different types of graphs

- Some graphs are **unweighted**. These represent situations where all relationships between entities have equal importance.

Different types of graphs

- Some graphs are **unweighted**. These represent situations where all relationships between entities have equal importance.
 - Ex: All connected words in a word ladder are one letter apart from one another.



Types of Graphs Summary

- **Directed:** Unidirectional relationships between nodes, represented with a pointed arrow.
- **Undirected:** Bidirectional relationships between nodes, represented with an arrow-less line.
- **Weighted:** Each edge is assigned a numerical "weight" representing its relative significance/strength.
- **Unweighted:** Each edge has equal significance, no labels assigned.

Revisiting Graph Examples

Revisiting Graph Examples: Social Network

Properties

- Nodes: ???
- Edges: ???
- Undirected or Directed?
- Unweighted or Weighted?



Revisiting Graph Examples: Social Network

Properties

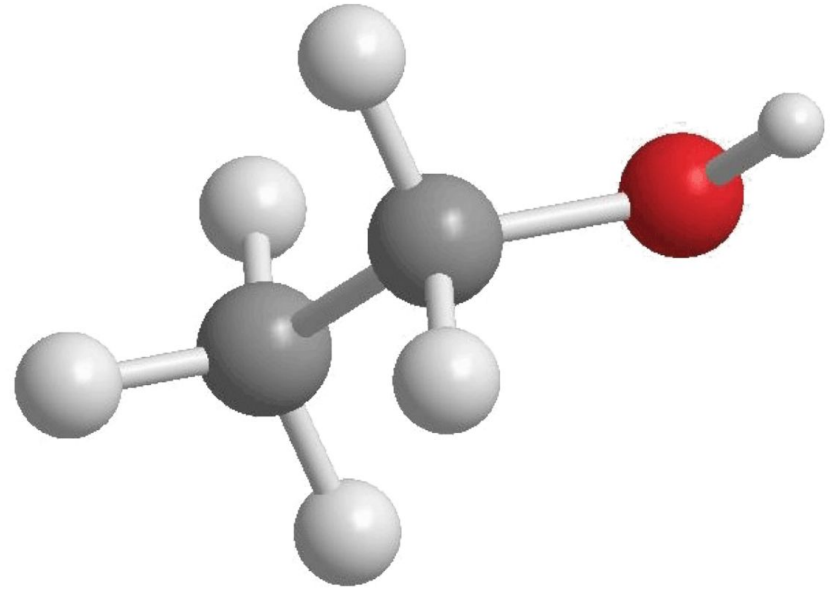
- Nodes: People
- Edges: "Friendship" or "Following"
- Undirected (Facebook) or Directed (Instagram)
- Unweighted



Revisiting Graph Examples: Chemical Bonds

Properties

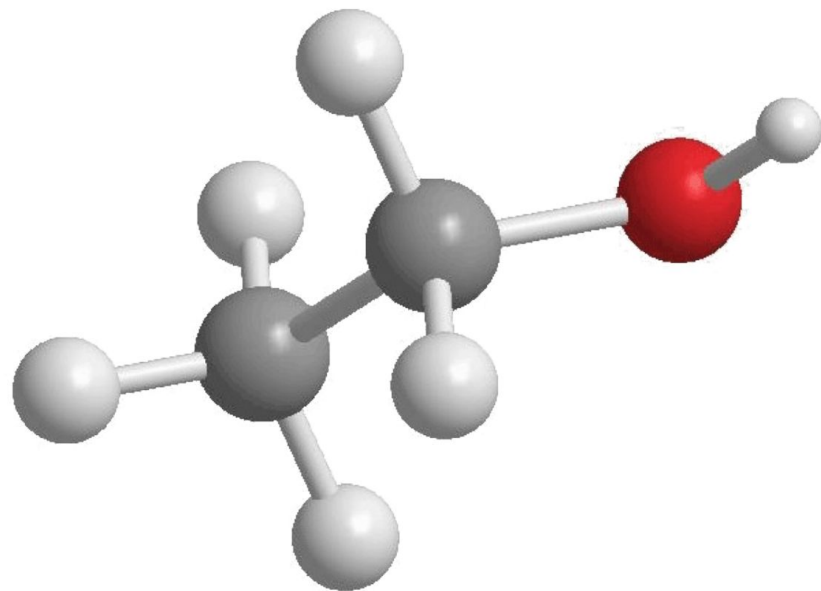
- Nodes: ???
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Revisiting Graph Examples: Chemical Bonds

Properties

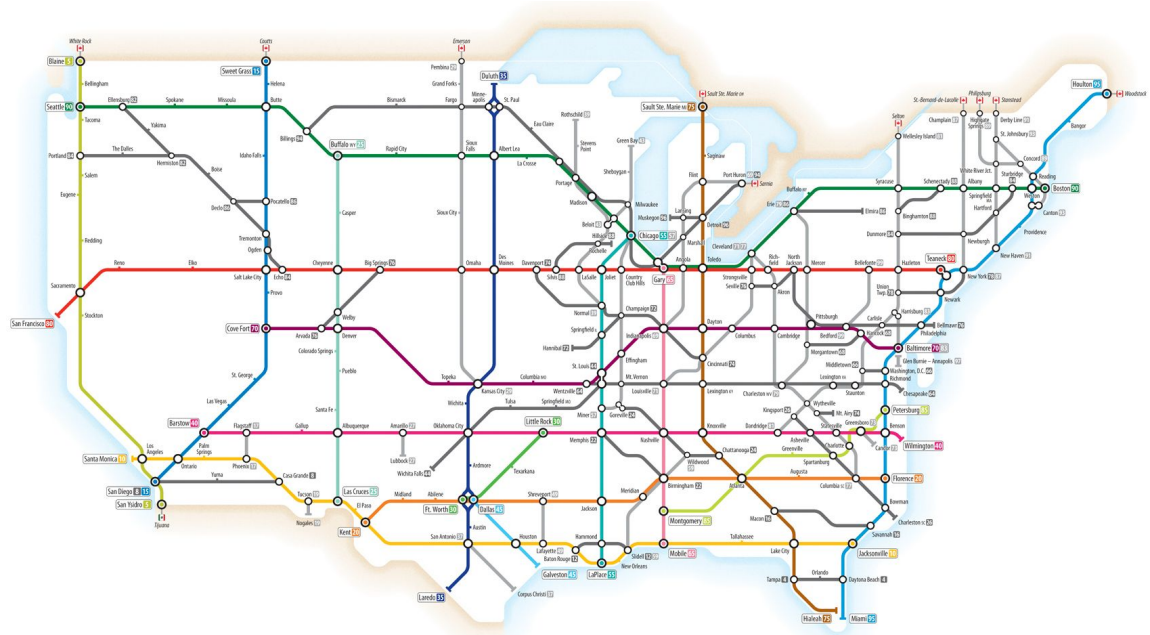
- Nodes: Atoms
- Edges: Bonds
(covalent or ionic)
- Undirected
- Weighted



Revisiting Graph Examples: Interstate Highways

Properties

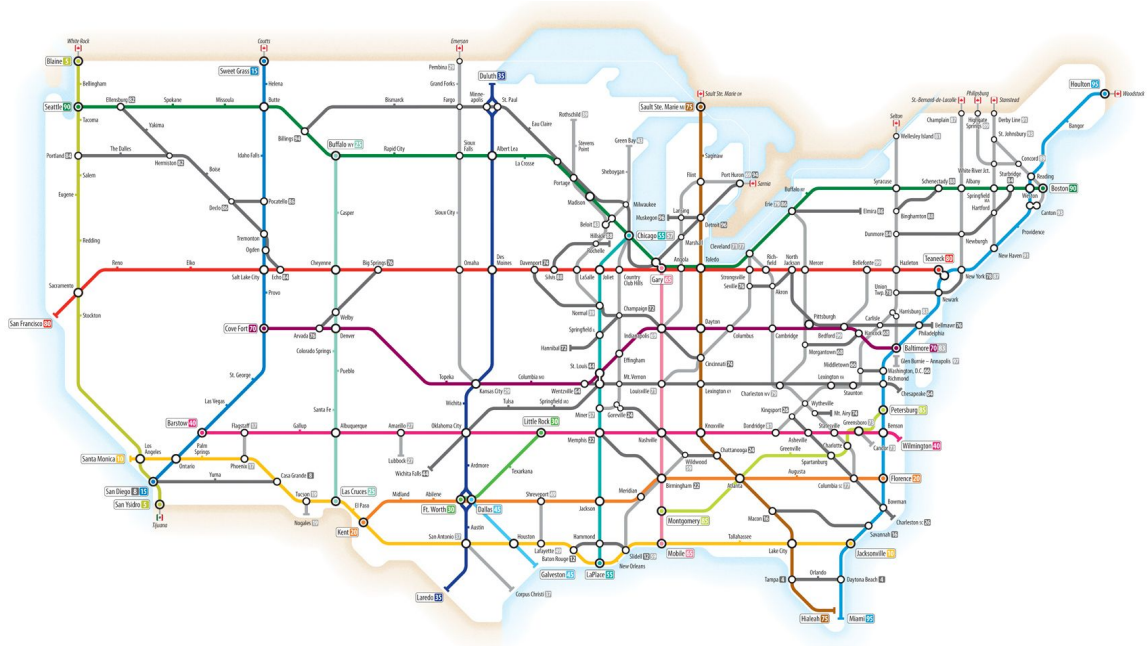
- Nodes: ???
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Revisiting Graph Examples: Interstate Highways

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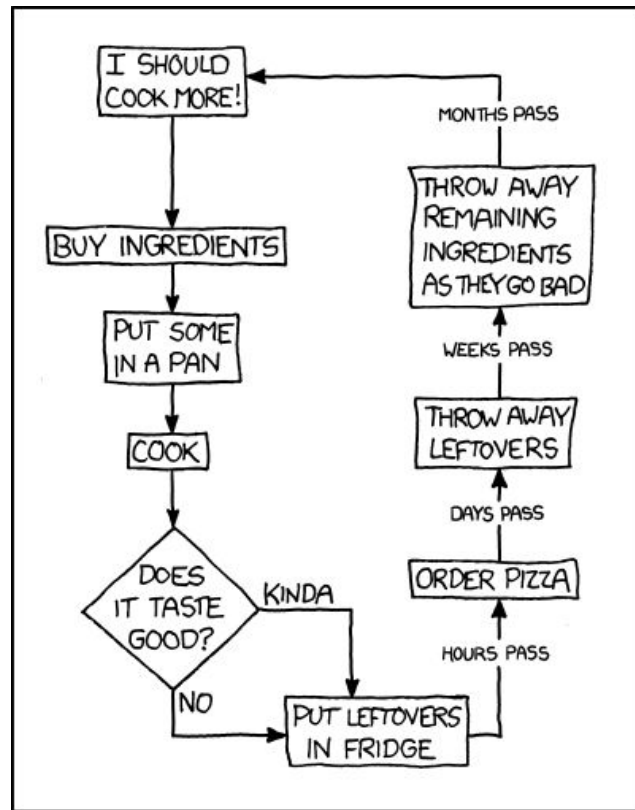
- Nodes: Cities
- Edges: Highways/roads
- Undirected
- Weighted



Revisiting Graph Examples: Flowcharts

Properties

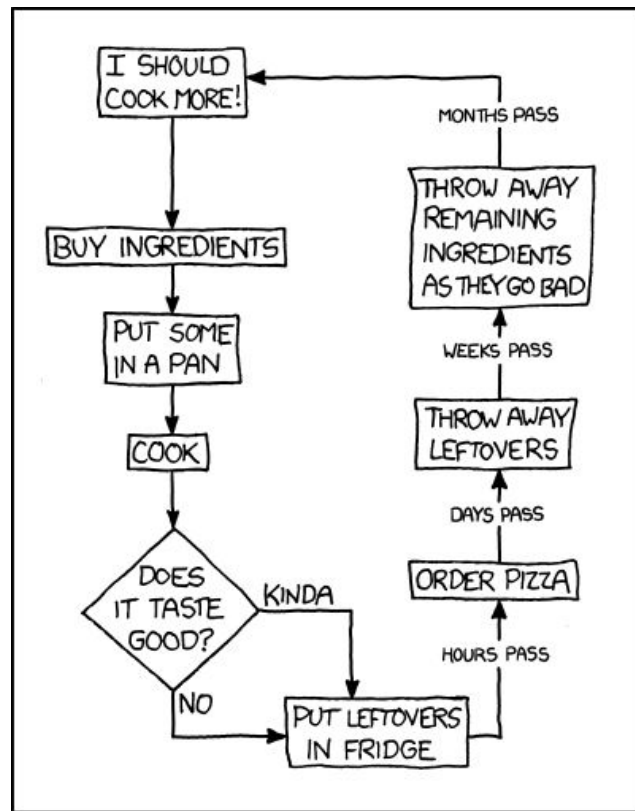
- Nodes: ???
- Edges: ???
- Undirected or Directed?
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Revisiting Graph Examples: Flowcharts

Properties

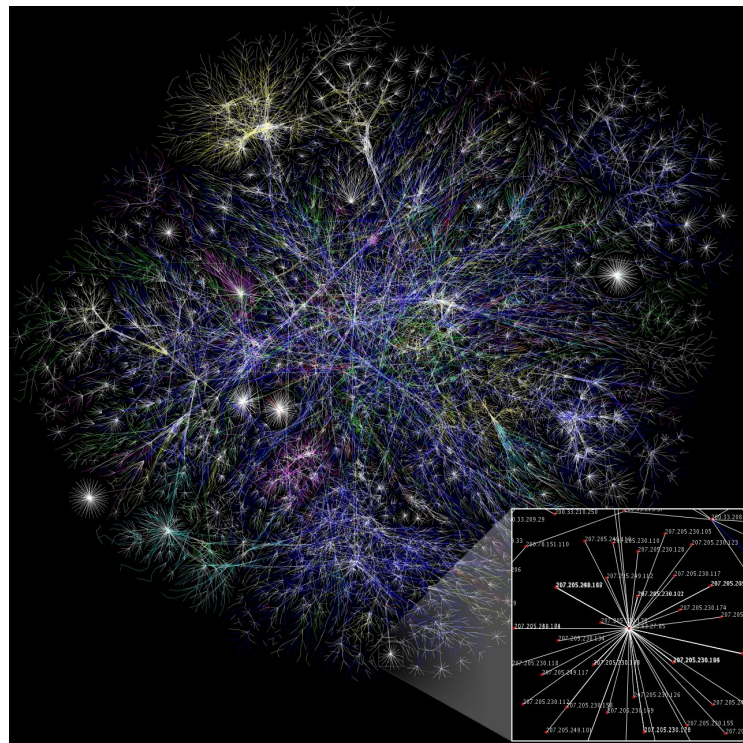
- Nodes: Events/Actions
- Edges: Transitions
- Directed
- Unweighted



Revisiting Graph Examples: The Internet

Properties

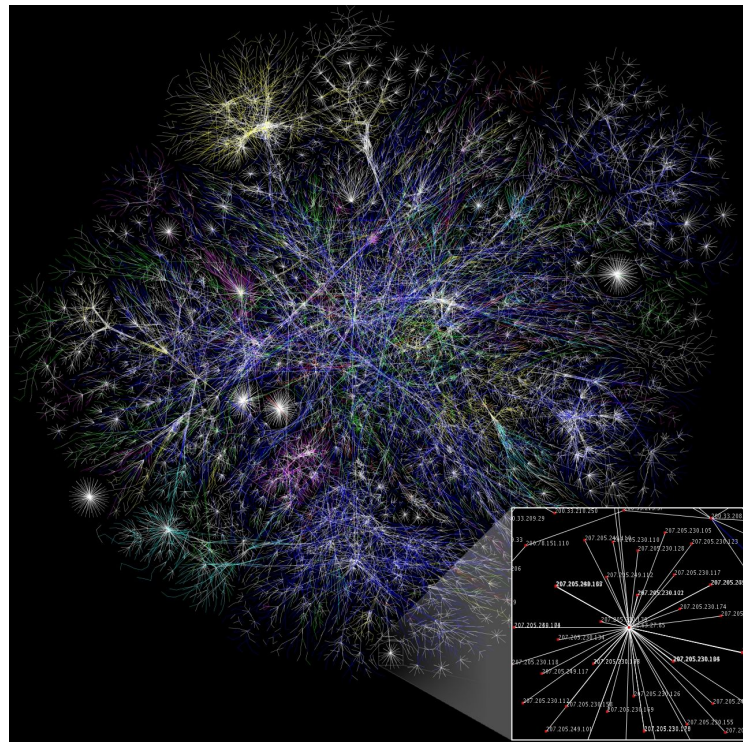
- Nodes: ???
- Edges: ???
- Undirected or Directed?
- Unweighted or Weighted?



Revisiting Graph Examples: The Internet

Properties

- Nodes: Devices (phones, computers, etc.)
- Edges: Connection pathways (Bluetooth, WiFi, Ethernet, cables)
- Undirected
- Can be weighted or unweighted



Graphs as Linked Data Structures

Putting it All Together

- We've seen nodes connected by edges (links) before when discussing linked lists and trees. These, along with graphs, are all **linked data structures!**

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- What differentiates each of these linked data structures?
 - **Linked lists:** Linear structure, each node connected to at most one other node.
 - **Trees:** Nodes can connect to multiple other nodes, no cycles, parent/child relationship and a single, special root node.

Putting it All Together

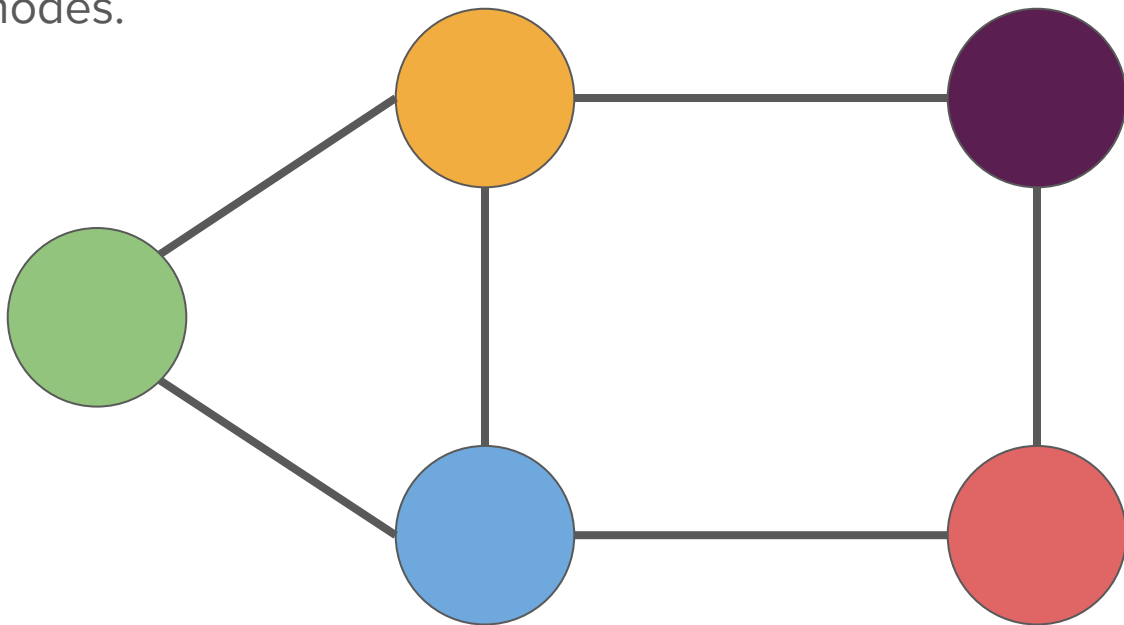
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- What differentiates each of these linked data structures?
 - **Linked lists:** Linear structure, each node connected to at most one other node.
 - **Trees:** Nodes can connect to multiple other nodes, no cycles, parent/child relationship and a single, special root node.
 - **Graphs:** No restrictions. It's the wild, wild west of the node-based world!

The Wild World of Graphs

- Graphs can have cycles, and there is no notion of a parent-child relationship between nodes.

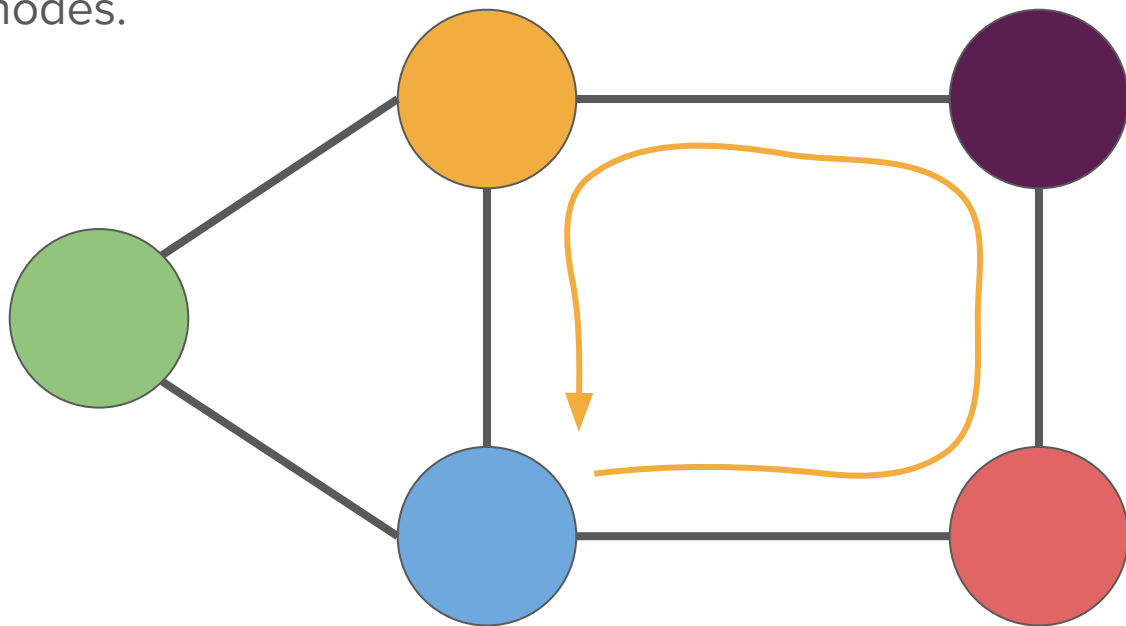
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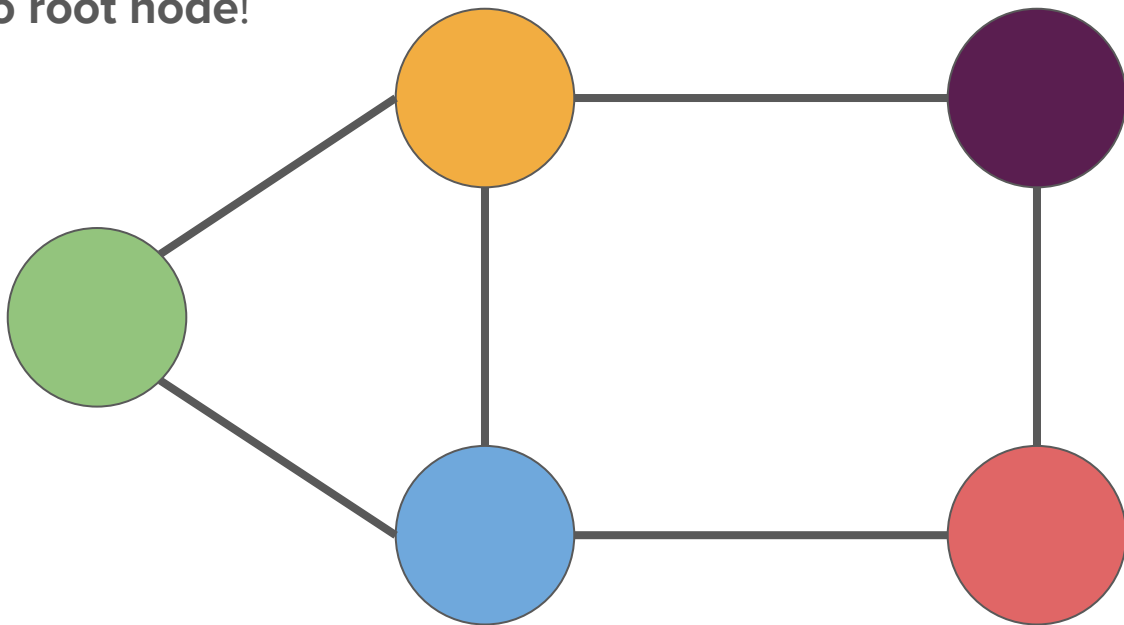
The Wild World of Graphs

- Graphs can have **cycles**, and there is no notion of a parent-child relationship between nodes.



The Wild World of Graphs

- Graphs have no nodes that are more important than other nodes. In particular, **there is no root node!**



Graphs are the most *powerful, flexible, and expressive* abstraction that we can use to *model relationships between different distributed entities*. You will find graphs everywhere you look!

Representing Graphs

How do we store and represent graphs in code?

Attendance ticket:

<https://tinyurl.com/106bGraphs>

Please don't send this link to students who are not here. It's on your honor!

The **Node** struct

```
struct Node {  
    string data;  
    Node* next;  
}
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How would our data be different for each application?

The **Node** struct

```
struct Node {  
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```

How can we better represent our edges in graphs?

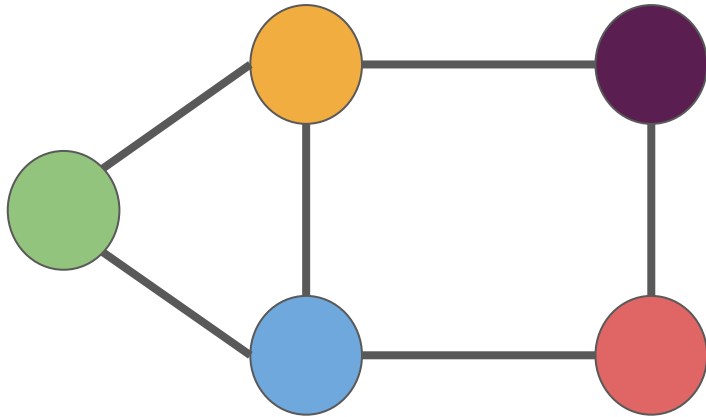
Approach 1: Adjacency List

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- We can represent a graph as a map from nodes to the collection of nodes that each node is adjacent to.

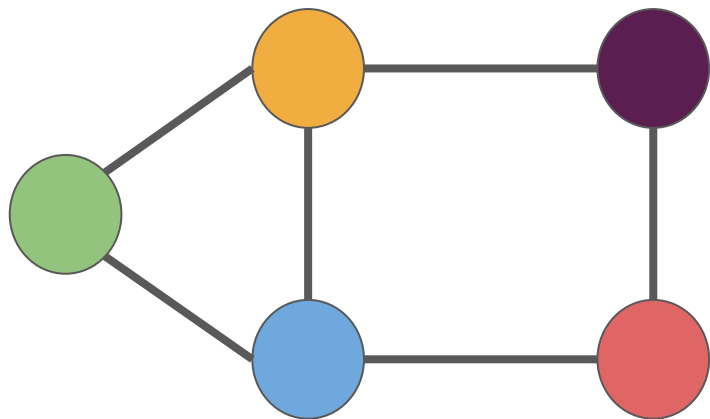
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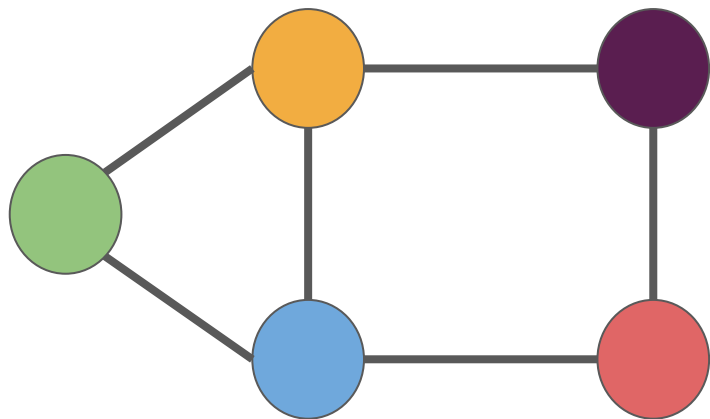
Map<Node, Set<Node>>

Node	Set<Node>>
Node	Adjacent to






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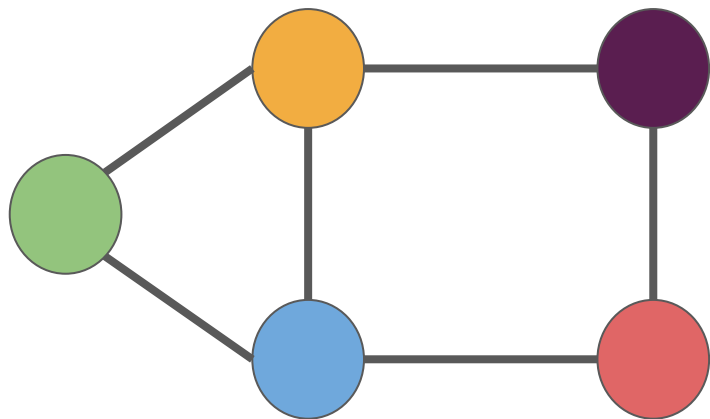


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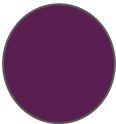
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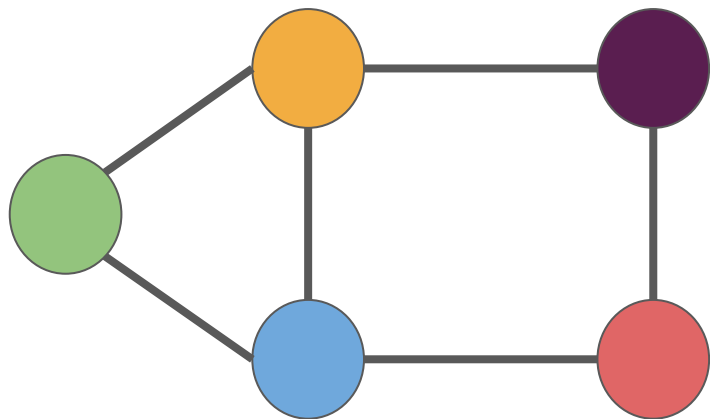


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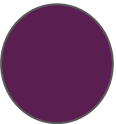


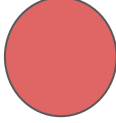

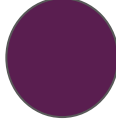


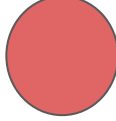
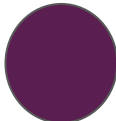

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- The approach we just saw is called an adjacency list and comes in a number of different forms:
 - `Map<Node, Set<Node>>`
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- How might you incorporate weights?

Approach 1: Adjacency List

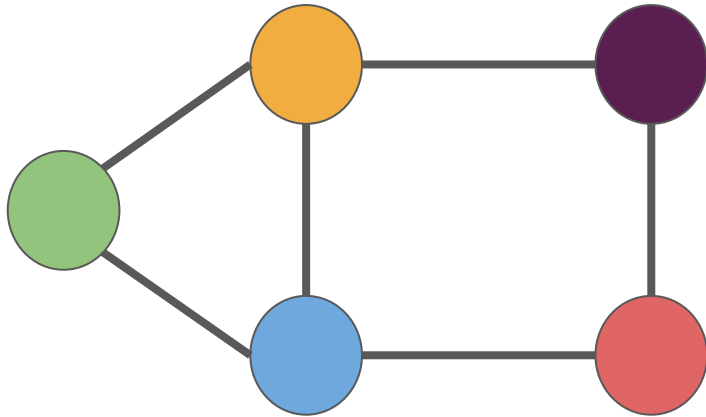
- The approach we just saw is called an adjacency list and comes in a number of different forms:
 - `Map<Node, Set<Edge>>`
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 - `Vector<Node>` <- in this case, the Node struct holds collection of its adjacent neighbors
- The core idea is that we have some kind of mapping associating each node with its outgoing edges (or neighboring nodes).
- **Create an Edge struct that holds both a Node and a weight**

Approach 2: Adjacency Matrix

- We can also use a two-dimensional matrix to represent the relationships in a graph.

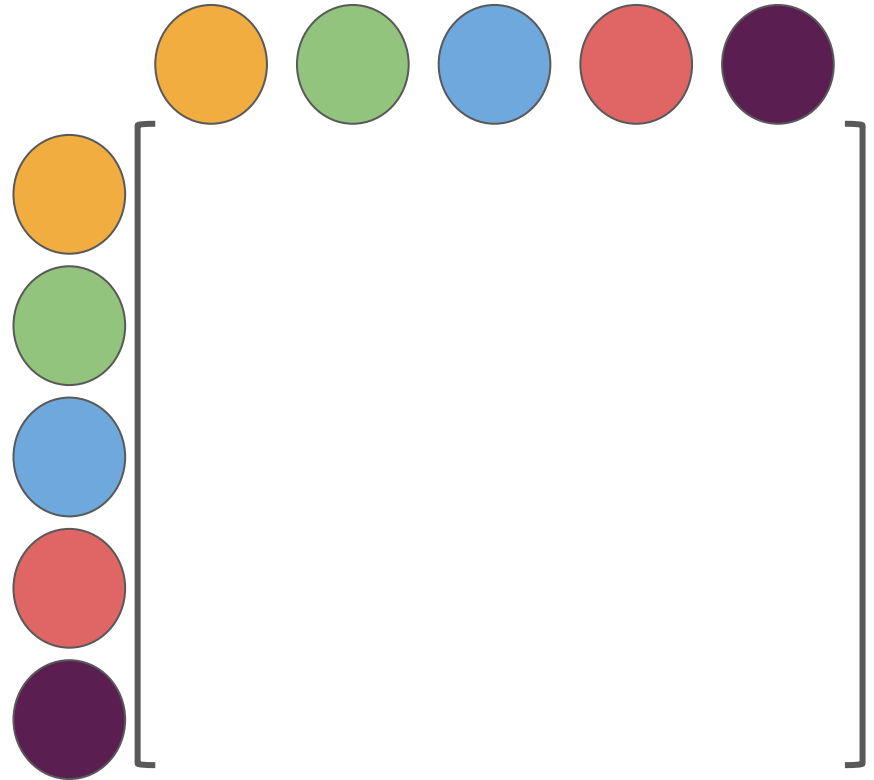
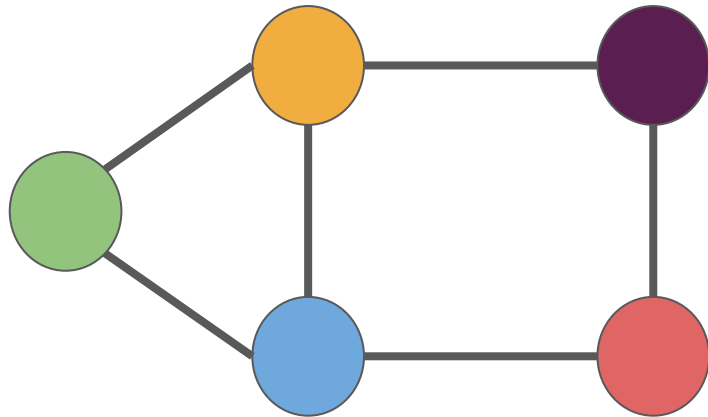
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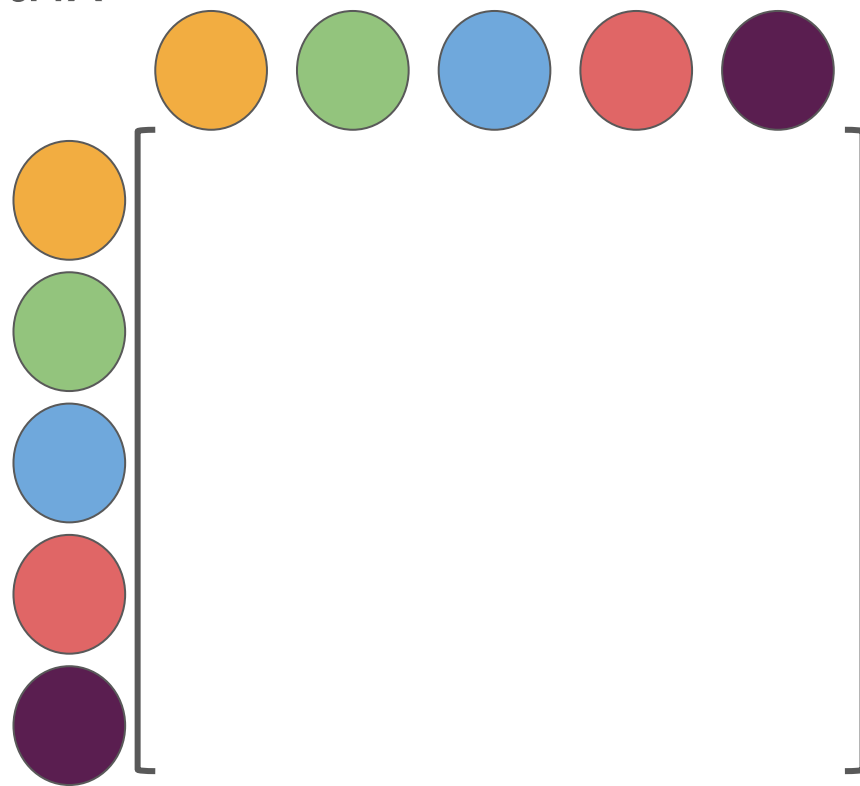
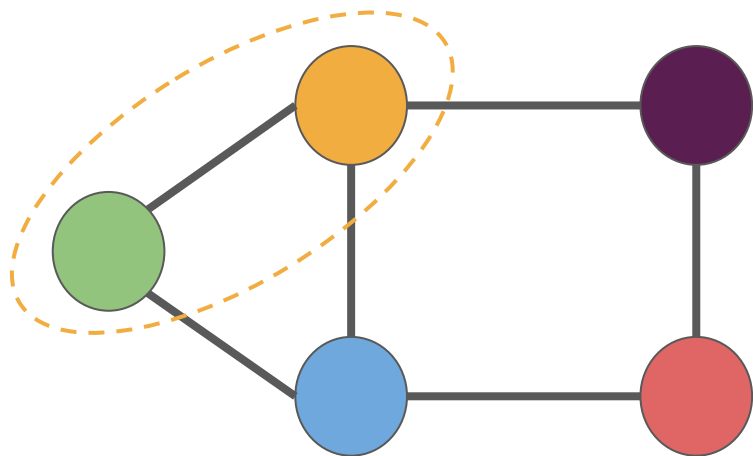
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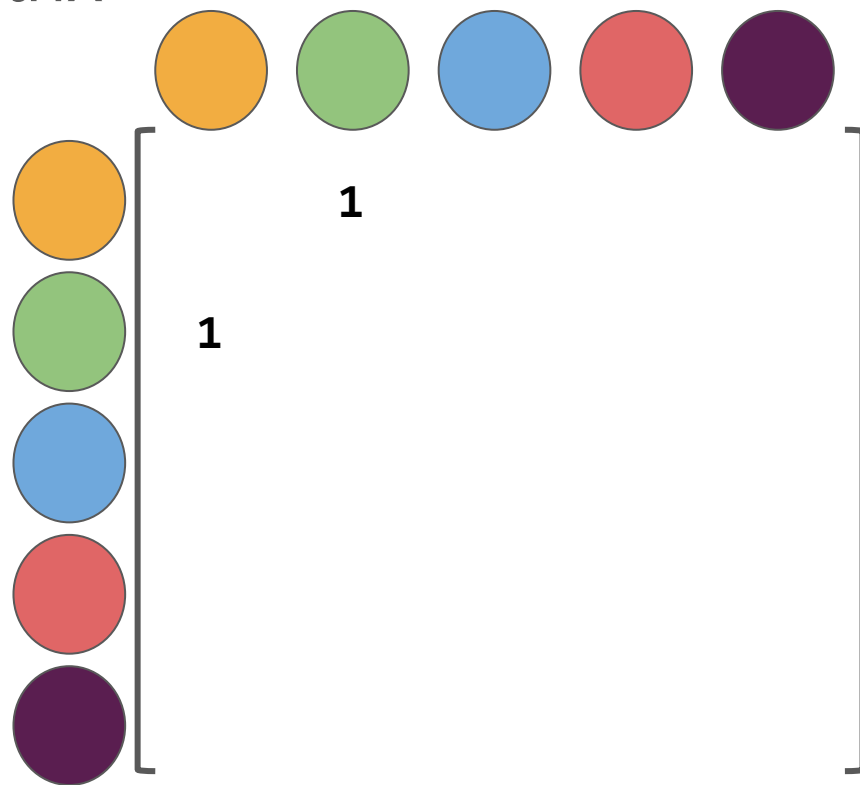
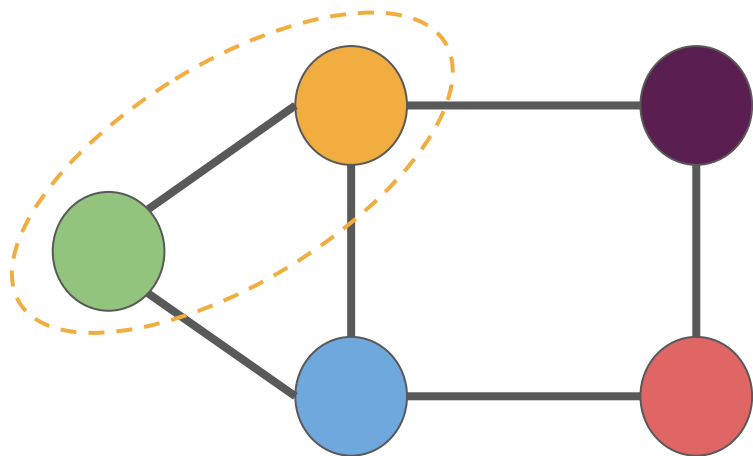
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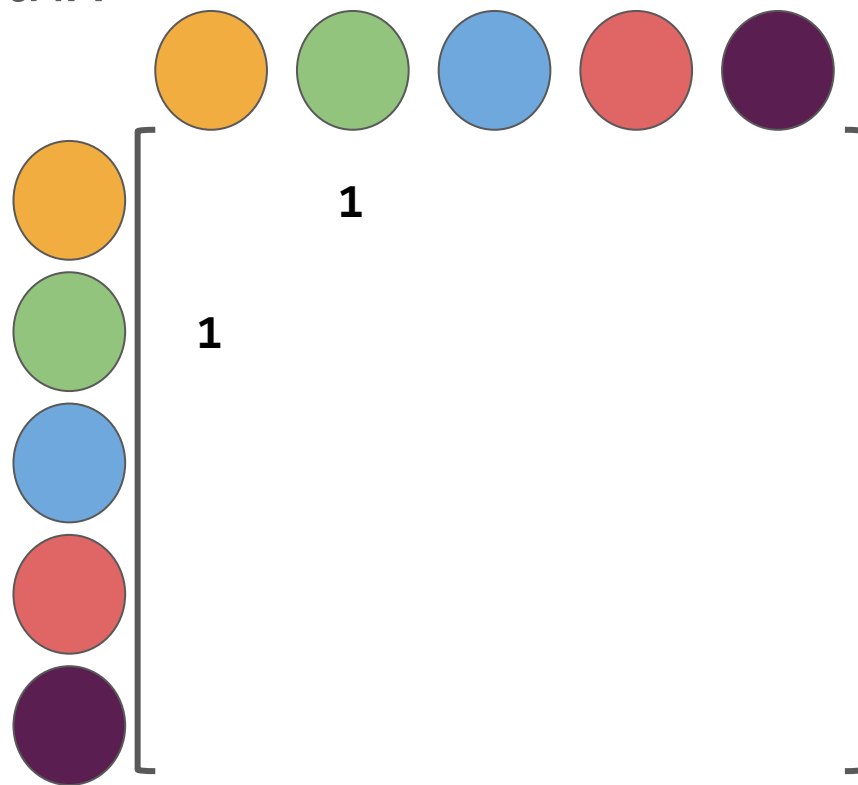
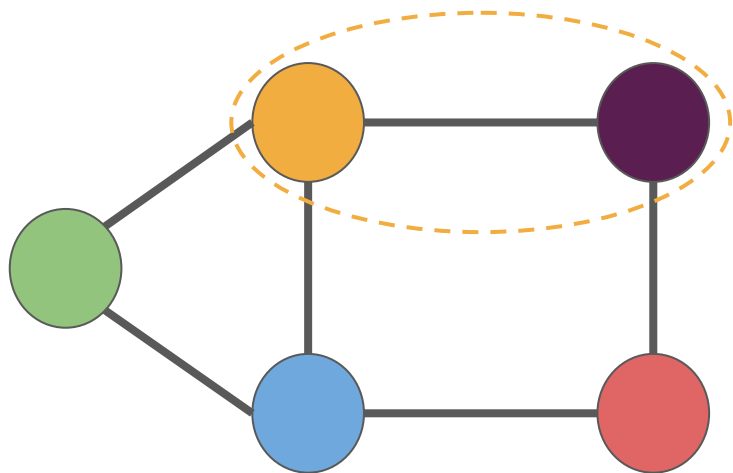
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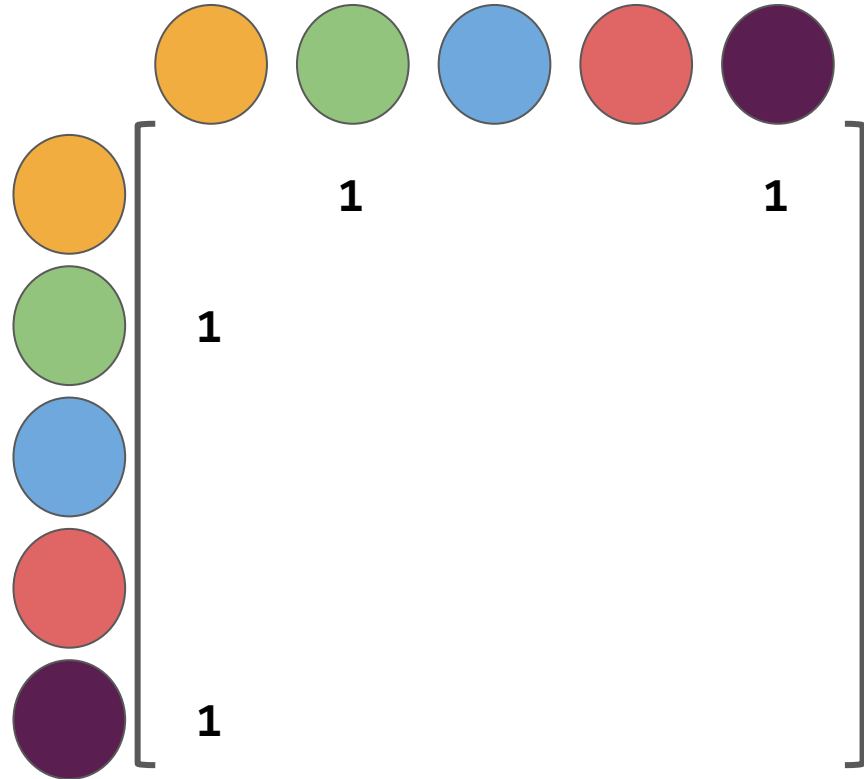
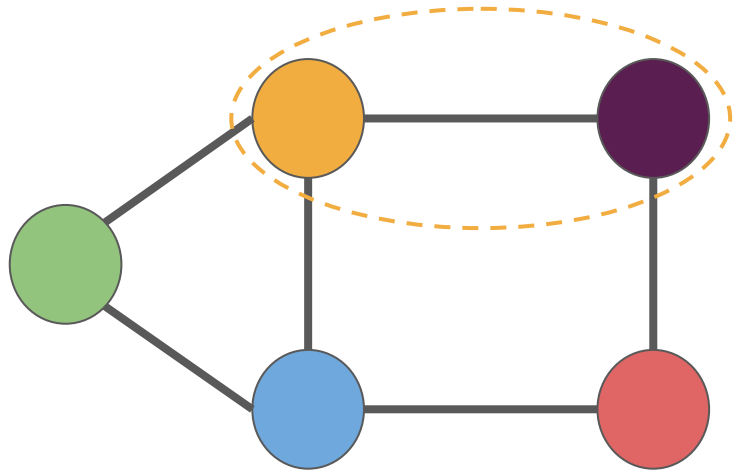
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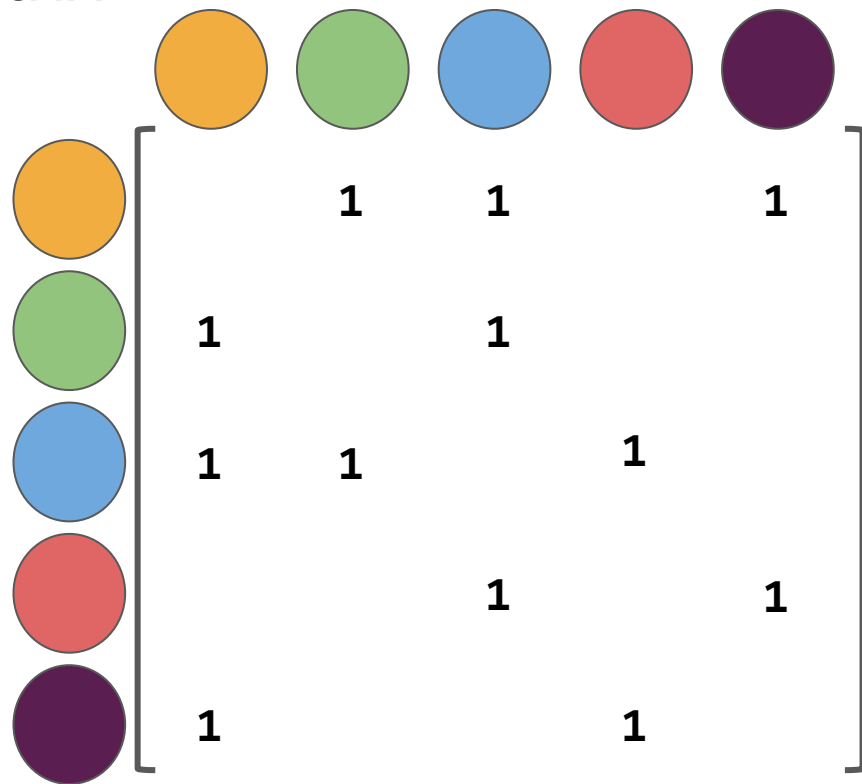
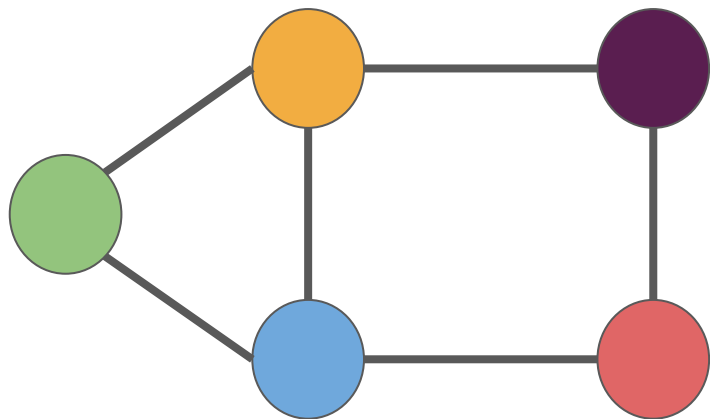
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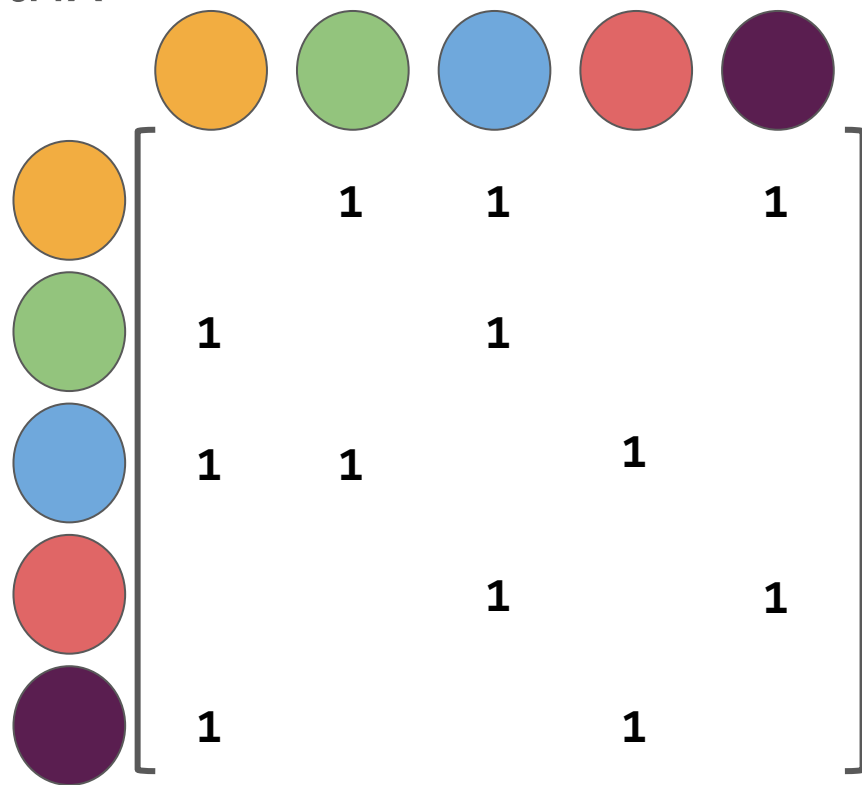
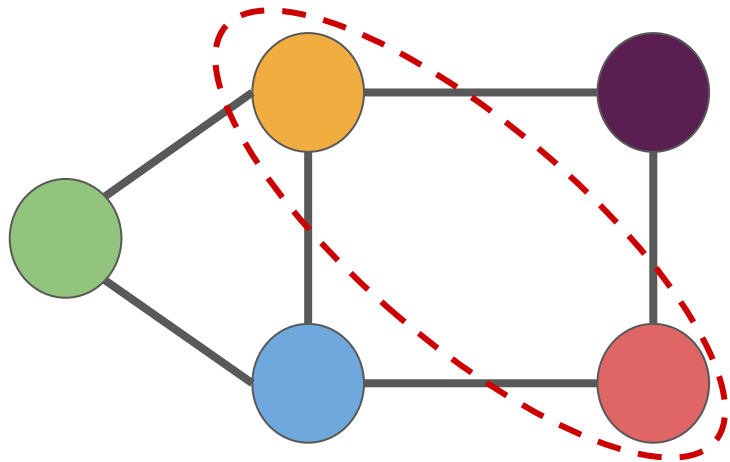
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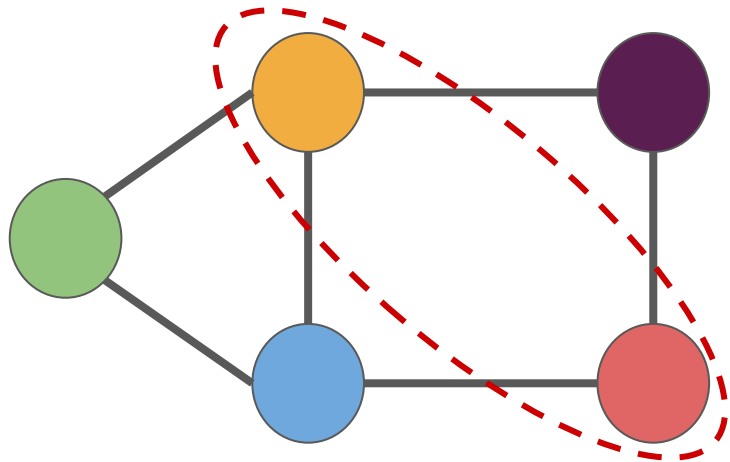
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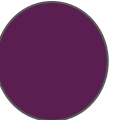


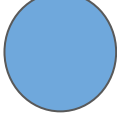
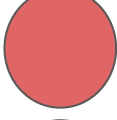
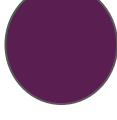
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		1	1	0	1
	1		1		
	1	1		1	
	0		1		1
	1			1	

Approach 2: Adjacency Matrix

- To add weights, store other numbers besides 1 in the matrix.
- Adjacency matrices are beneficial when our graph isn't **sparse**, i.e. there aren't a lot of 0s. Otherwise, storing a mostly-0s matrix is not space efficient.
- Other benefits:
 - Grid lookup is super fast!
 - Storing weights is more straightforward than in the adjacency list.
 - Computer hardware has been optimized for matrix math - so using a grid can help us perform complex matrix operations for data analysis.

Graph Algorithms

Graph Algorithms

- There are [many, many different graph algorithms](#) out there.
 - Check out this [graph search algorithms demo](#).

Graph Algorithms

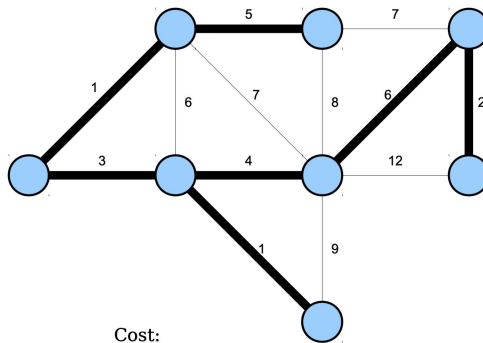
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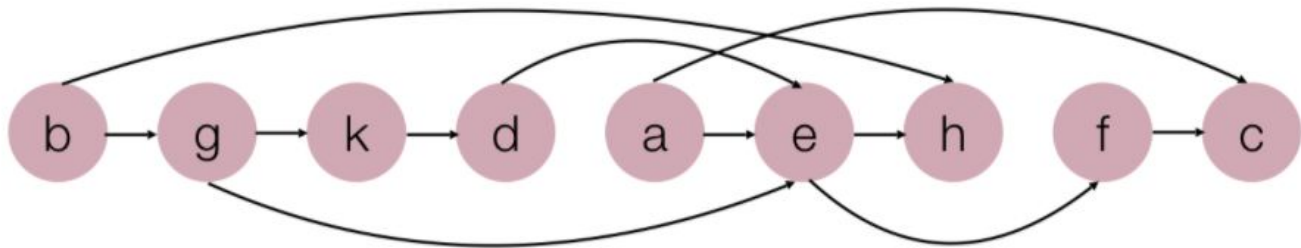
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Cost:
 $1 + 3 + 5 + 4 + 1 + 6 + 2 = 22$

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 - **Topological Sort:** "Sort" the nodes in a dependency graph in such a way that traversing the nodes in order results in all dependencies being fulfilled at each point in time.
 - **Traveling salesman:** Given a map of cities and the distances between them, find the shortest path that traverses all cities in the map.
- Graphs can also be used in conjunction with machine learning algorithms to accomplish cool things. Take CS224W to learn more!

Announcements

Announcements

- Assignment 5 revisions and Assignment 6 are due today at 11:59pm PDT. Remember that this is a hard deadline, and there is no grace period!
- There is no official section this week, but keep an eye out for an email from your SL's in case they are hosting an optional section, or if the section time is being used for Final Project presentations.
- Submit questions for tomorrow's Ask Us Anything [here](#) (also in this week's announcements). No lecture on Thursday so tomorrow is our last day of class.
- Tomorrow will be our last group OH (Kylie and Jenny will be there!).

Making our own projects!

```
#include "vector.h"
```

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○ 'vector.h' file not found

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?????????

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Google

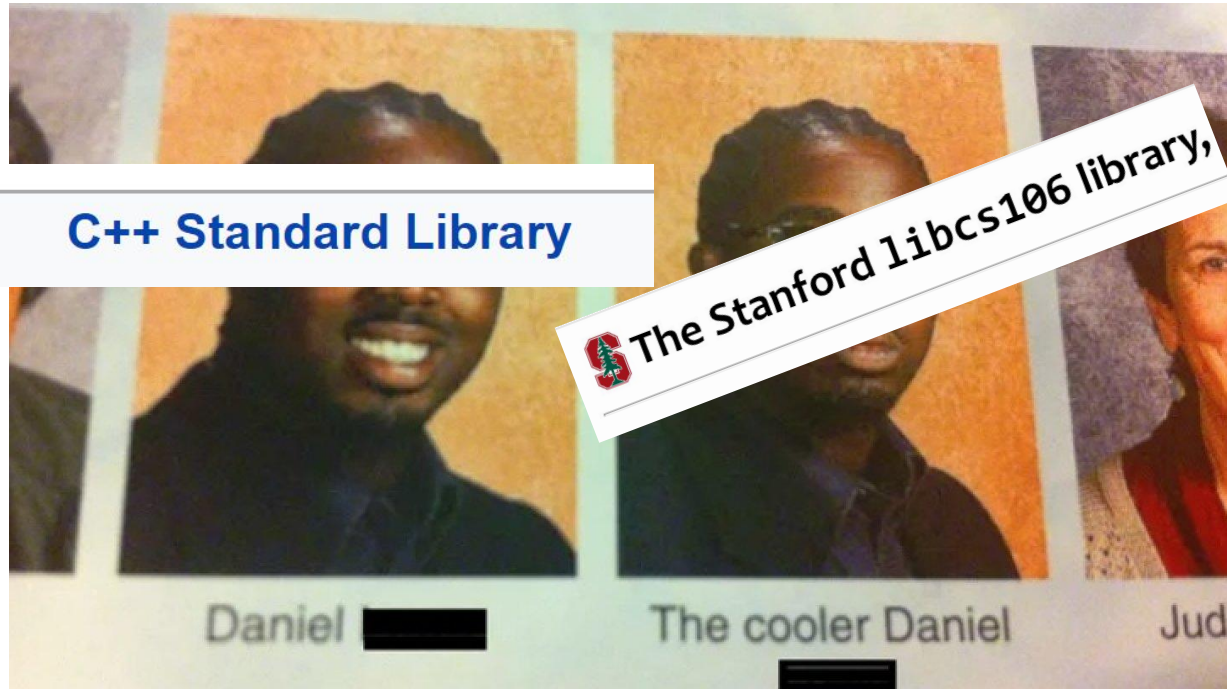
stanford lied to me how to sue???



The Standard Template Library

“using namespace std??”

What we know so far



How do I use STL ADTs?

A 5 step guide:

1. Include your ADT

How do I use STL ADTs?

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1. Include your ADT
 - a. `#include <vector>`

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2. Write the ADT in lowercase

How do I use STL ADTs?

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4. ???
5. Profit!

Spot the difference!

What you want to do	Stanford <code>Vector<int></code>	<code>std::vector<int></code>
Create a new, empty vector	<code>Vector<int> vec;</code>	<code>std::vector<int> vec;</code>
Create a vector with <code>n</code> copies of 0	<code>Vector<int> vec(n);</code>	<code>std::vector<int> vec(n);</code>
Create a vector with <code>n</code> copies of a value <code>k</code>	<code>Vector<int> vec(n, k);</code>	<code>std::vector<int> vec(n, k);</code>
Add a value <code>k</code> to the end of a vector	<code>vec.add(k);</code>	<code>vec.push_back(k);</code>
Remove all elements of a vector	<code>vec.clear();</code>	<code>vec.clear();</code>
Get the element at index <code>i</code>	<code>int k = vec[i];</code>	<code>int k = vec[i];</code> (does not bounds check)
Check size of vector	<code>vec.size();</code>	<code>vec.size();</code>
Loop through vector by index <code>i</code>	<code>for (int i = 0; i < vec.size(); ++i) ...</code>	<code>for (std::size_t i = 0; i < vec.size(); ++i) ...</code>
Replace the element at index <code>i</code>	<code>vec[i] = k;</code>	<code>vec[i] = k;</code> (does not bounds check)

Table courtesy of Frankie Cerkenik and Sathya Edamadaka!

Makefiles

How does our code actually compile?

Makefiles and cmake

A Makefile is the recipe for your build!

It tells the compiler:

- What files to include
- What dependencies they have
- What code to run to put it all together

```
targets: prerequisites  
  command  
  command  
  command
```

Makefiles and cmake

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It tells the compiler:

- What files to include
- What dependencies they have
- What code to run to put it all together

These can be a little manual – **cmake** abstracts a lot of it for you!

Example cmake file (from CS106L)

```
cmake_minimum_required(VERSION 3.0)
project(wikiracer)

set(CMAKE_CXX_STANDARD 17)
set(CMAKE_CXX_STANDARD_REQUIRED True)

find_package(cpr CONFIG REQUIRED)

# adding all files
add_executable(main main.cpp wikiscraper.cpp.o error.cpp)

target_link_libraries(main PRIVATE cpr)
```

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Take CS 107/107E next to learn more about compiling!

Leveling up classes

Speaking of `vector<int>`...

What's up with <>?

When we make classes, we can initialize them in the constructor with some parameters!

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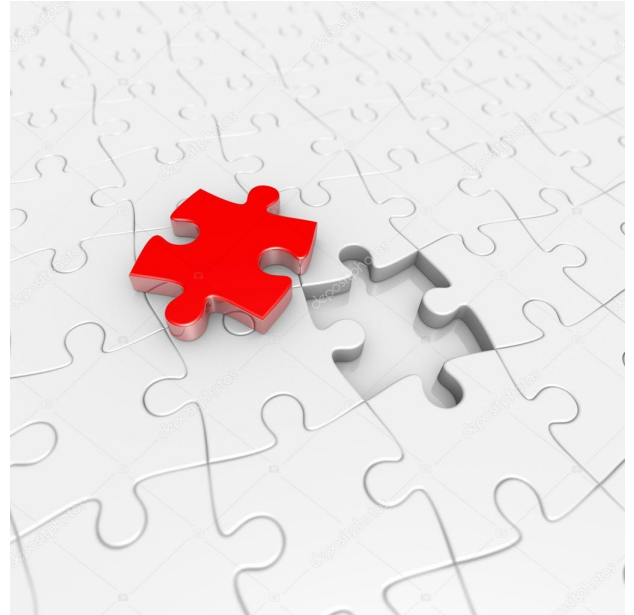
How can we make a class that can take in any type of parameters?

Template classes!

All of our favorite ADTs are template classes!

Pros:

- Can take in any type
- Generalized
- Easy for the client and the programmer



Template classes!

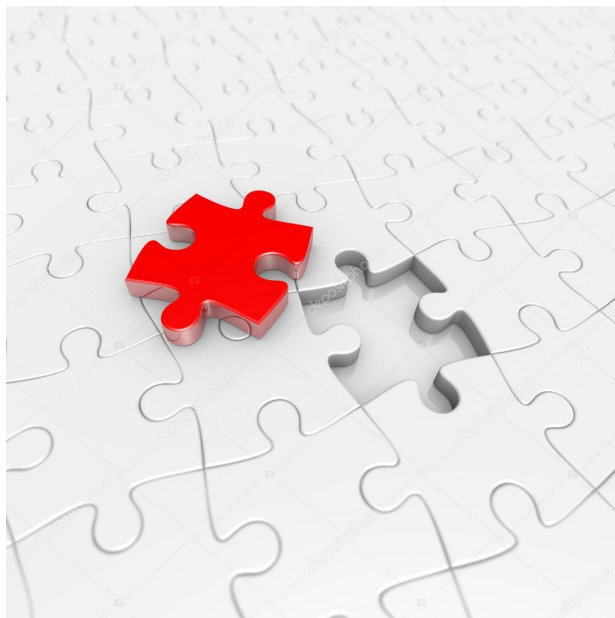
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Pros:

- Can take in any type
- Generalized
- Easy for the client and the programmer

Cons:

- We don't know how to make them yet??



Syntax

Instead of:

- `class` ClassName { ... }
- `FIXED_TYPE` var;

Use:

- `template<class typeName> class`
ClassName { ... }
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- `class` ClassName { ... }
- `FIXED_TYPE` var;

Use:

- `template<class typeName> class`
ClassName { ... }
- `typeName` var;

Anywhere you use a fixed type, use `typeName`!

What about operators?

Want to learn more?

Take CS106L!

havenw@stanford.edu

Go forth and code!

What's next?

Roadmap

C++ basics

User/client

vectors + grids

stacks + queues

sets + maps

Core
Tools

testing

algorithmic
analysis

recursive
problem-solving

Object-Oriented
Programming

Implementation

arrays

dynamic memory
management

linked data structures

real-world
algorithms

Life after CS106B!

Diagnostic

